# EECS16A Imaging 2

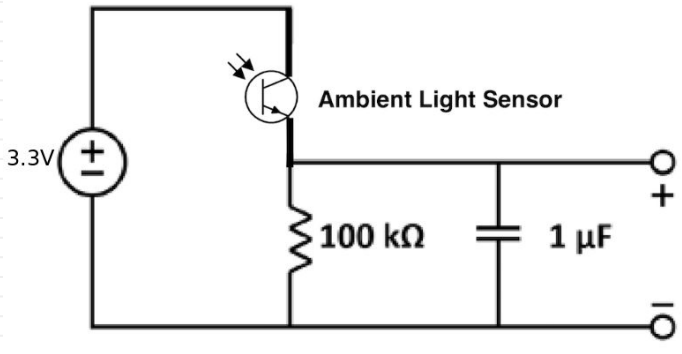
# Agenda

- Quick overview + review
- Images as matrices and vectors
- Pixel-by-pixel scanning
- Reconstructing scans as images
- Lab-specific simulation directions

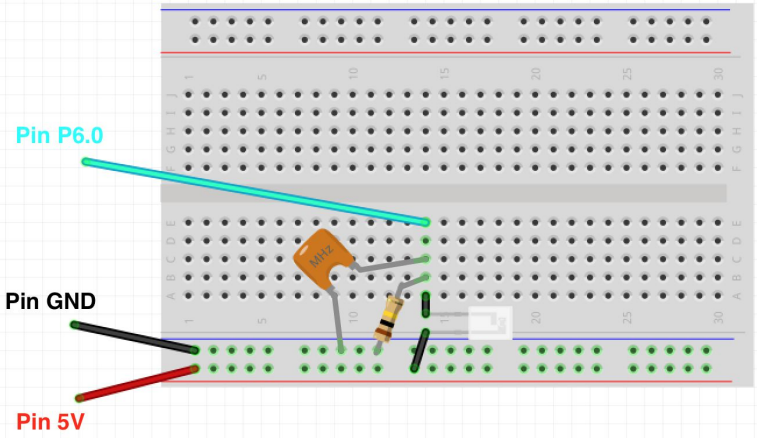
# Last Week: Imaging 1

- Built our very first circuit!
  - **What did this circuit do?**

**Circuit Diagram**




**Breadboard Diagram**



# Today's Lab: Single Pixel Scanning

- Circuit from last week measures **light** intensity
- Simulated projector illuminates image in a controlled way
- Python programming to reconstruct image

# Why?

- Imaging 1:
  - Finding a link between physical quantities and voltage is powerful
  - If you can digitize it, you can do anything (IOT devices, internet, code, processing)
- Imaging 2:
  - What measurements are good measurements?
    - Remember Kody and Nara from Dis0C?

# Kody and Nara

**2. Finding The Bright Cave**

Nara the one-handed druid and Kody the one-handed ranger find themselves in dire straits. Before them is a cliff with four cave entrances arranged in a square: two upper caves and two lower caves. Each entrance emits a certain amount of light, and the two wish to find exactly the amount of light coming from each cave. Here's the catch: after contracting a particularly potent strain of ghoul fever, our intrepid heroes are only able to see the total intensity of light before them (so their eyes operate like a single-pixel camera). Kody and Nara are capable adventurers, but they don't know any linear algebra – and they need your help.

Kody proposes an imaging strategy where he uses his hand to completely block the light from two caves at a time. He is able to take measurements using the following four masks (black means the light is blocked from that cave):

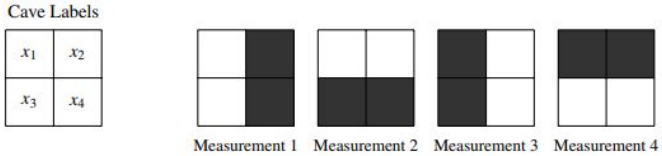



Figure 1: Four image masks.

(a) Let $\vec{x}$ be the four-element vector that represents the magnitude of light emanating from the four cave entrances. Write a matrix $\mathbf{K}$ that performs the masking process in Figure 1 on the vector $\vec{x}$, such that $\mathbf{K}\vec{x}$ is the result of the four measurements.

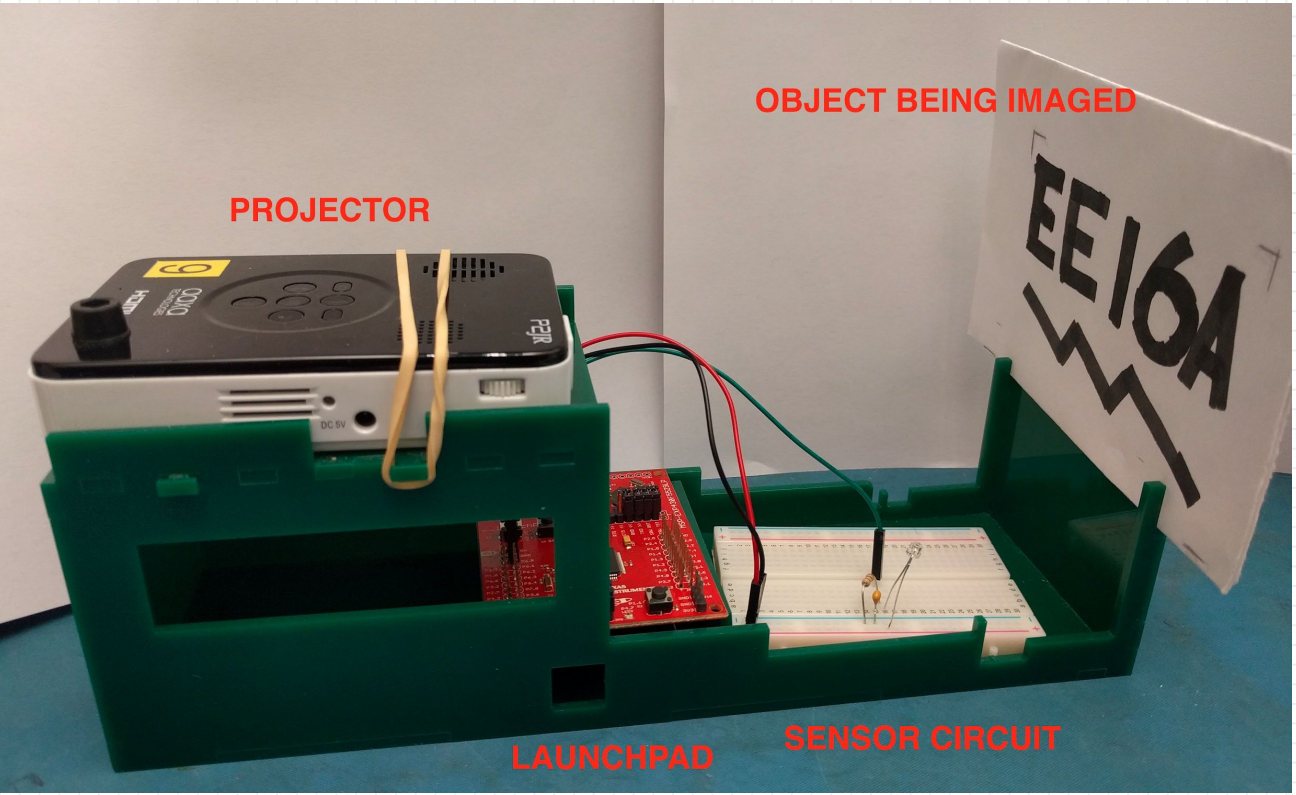
(b) Does Kody's set of masks give us a unique solution for all four caves' light intensities? Why or why not?

(c) Nara, in her infinite wisdom, places her one hand diagonally across the entrances, covering two of the cave entrances. However, her hand is not wide enough, letting in 50% of the light from the caves covered and 100% of the light from the caves not covered. The following diagram shows the percentage of light let through from each cave:

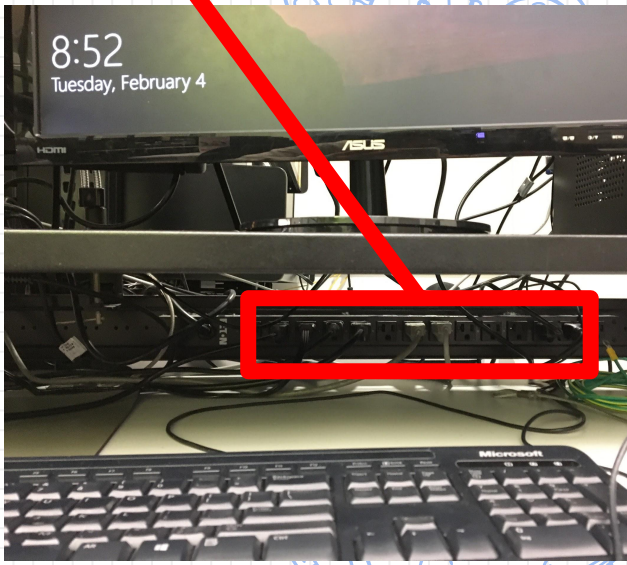
# Illuminating the Big Picture

- Linear dependence
  - When can you recover your image?
  - Does it matter what mask matrix you pick?
  - Does it matter how you cover the pixels?
- Invertibility
  - When can you solve Ax = b?
  - How does this relate to our system?
  - How does this affect the way we pick our masking matrix?

# Real-life Setup



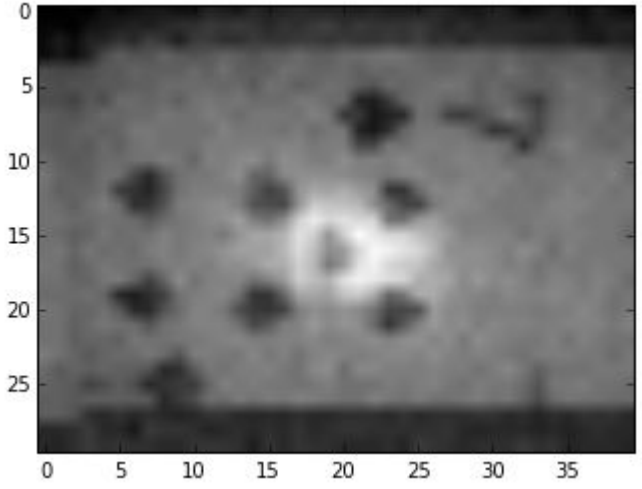

Power strip to power your projector



# Real-life Setup (cont.)

1. Draw a “simple” image
2. Project masks (rows of H) onto it in a dark environment
3. Measure ambient light sensor reading **s**
4. Multiply by H inverse to find **i** (= $H^{-1}$.**s**)

# Sample Real-Life Setup Images



# This Lab: Software Simulator Setup

1. **Upload (“simple”) image of an object (or use default)**
2. **Shrink your image (preferably 32x32)**
3. ‘Project’ masks (rows of H) onto it and “measure” **s** using matrix multiplication
4. Multiply by H inverse to find **i** (= $H^{-1}$**s**)

# Images, Matrices, Vectors

- What are the unknowns in our system?
- Want to do an experiment to get information about these unknowns
- We can do a lot of interesting processing on vectors, but we need to convert the image into one first
  - In lecture and discussion, you have seen how to turn an image into a vector. How?

# Images, Matrices, Vectors

| | |
|---|---|
| [0] | [1] |
| [2] | [3] |
| [4] | [5] |

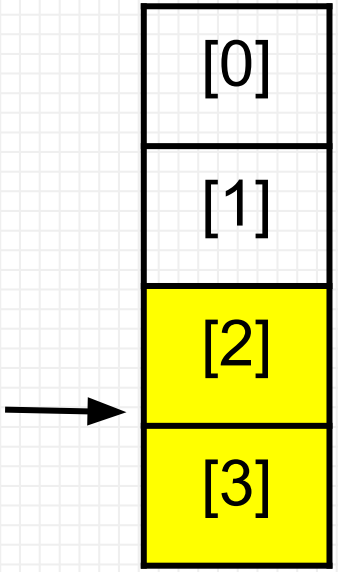
# Images, Matrices, Vectors

| [0] | [1] |
| --- | --- |
| [2] | [3] |
| [4] | [5] |

| [0] |
| --- |
| [1] |

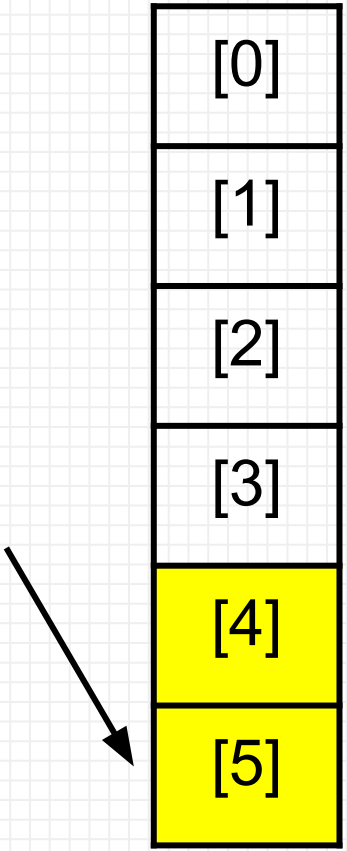
# Images, Matrices, Vectors

| | |
|---|---|
| [0] | [1] |
| [2] | [3] |
| [4] | [5] |



# Images, Matrices, Vectors

| | |
|---|---|
| [0] | [1] |
| [2] | [3] |
| [4] | [5] |



# Images, Matrices, Vectors

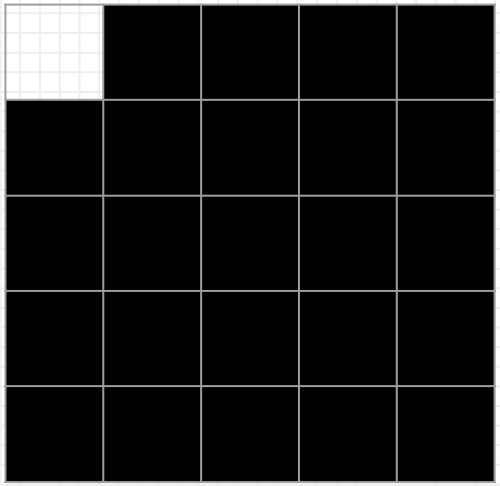
| | |
|---|---|
| [0] | [1] |
| [2] | [3] |
| [4] | [5] |

→

| |
|---|
| [0] |
| [1] |
| [2] |
| [3] |
| [4] |
| [5] |

# Pixel-by-Pixel Scan of an Image

# Pixel-by-Pixel Scan of an Image

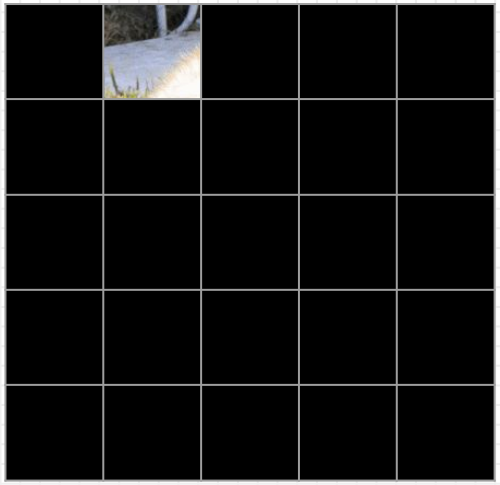


# Pixel-by-Pixel Scan of an Image

Masked image

Image

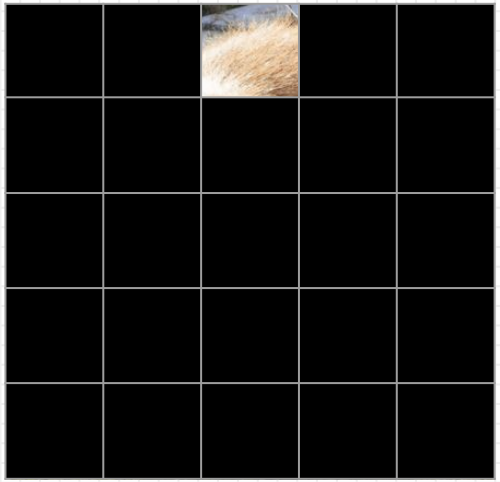
# Pixel-by-Pixel Scan of an Image



Masked image

Image

# Pixel-by-Pixel Scan of an Image



Masked image

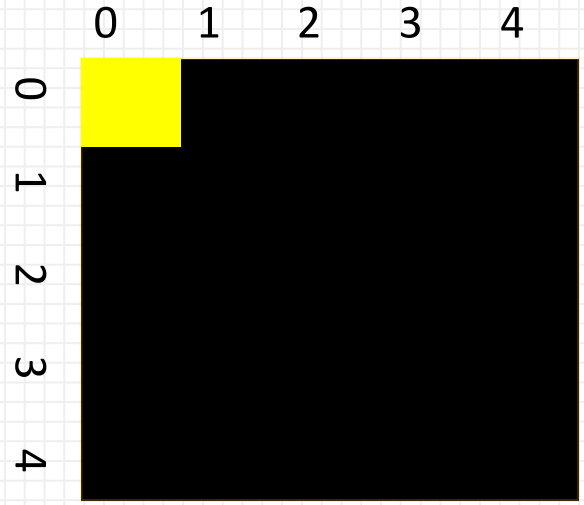
Image

## Question Time

- To read all the pixels of a 4x4 image, how many pixel-by-pixel scans do we need to do?

# Representing our Masks in Python

**Imaging Mask 0**




mask0 =

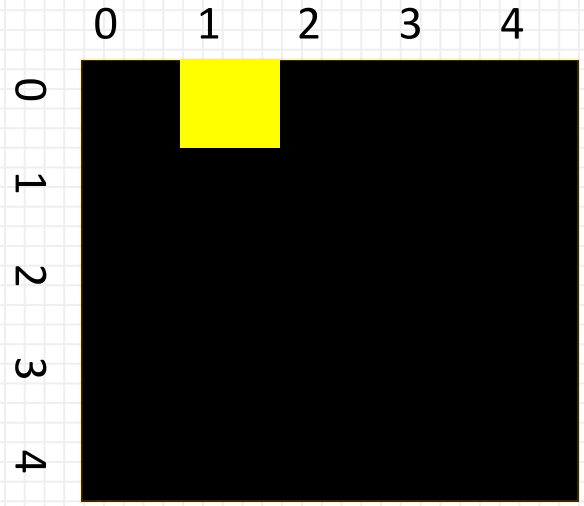
np.array([

| | | | | | |
|---|---|---|---|---|---|
| [ | **1,** | **0,** | **0,** | **0,** | **0** ] |
| [ | **0,** | **0,** | **0,** | **0,** | **0** ] |
| [ | **0,** | **0,** | **0,** | **0,** | **0** ] |
| [ | **0,** | **0,** | **0,** | **0,** | **0** ] |
| [ | **0,** | **0,** | **0,** | **0,** | **0** ]] |

)

# Representing our Masks in Python

**Imaging Mask 1**




mask1 =

np.array([

| | | | | | |
|---|---|---|---|---|---|
| [ | 0, | 1, | 0, | 0, | 0 ] |
| [ | 0, | 0, | 0, | 0, | 0 ] |
| [ | 0, | 0, | 0, | 0, | 0 ] |
| [ | 0, | 0, | 0, | 0, | 0 ] |
| [ | 0, | 0, | 0, | 0, | 0 ]] |

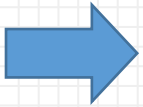
)

# Turning the Masks Into Vectors

5x5 mask to 25x1 vector

mask0 =

| | | | | | |
|---|---|---|---|---|---|
| [[ | 1, | 0, | 0, | 0, | 0 ], |
| [ | 0, | 0, | 0, | 0, | 0 ], |
| [ | 0, | 0, | 0, | 0, | 0 ], |
| [ | 0, | 0, | 0, | 0, | 0 ], |
| [ | 0, | 0, | 0, | 0, | 0 ]] |



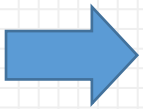
T

| | |
|---|---|
| Row 0 | 1 |
| Row 1 | 0 |
| Row 2 | 0 |
| Row 3 | 0 |
| Row 4 | 0 |
| ⋮ | |
| Row 24 | 0 |

# Turning the Masks Into Vectors

mask1 =

| | | | | | |
|---|---|---|---|---|---|
| [[ | 0, | 1, | 0, | 0, | 0 ], |
| [ | 0, | 0, | 0, | 0, | 0 ], |
| [ | 0, | 0, | 0, | 0, | 0 ], |
| [ | 0, | 0, | 0, | 0, | 0 ], |
| [ | 0, | 0, | 0, | 0, | 0 ]] |



T

| | |
|---|---|
| Row 0 | 0 |
| Row 1 | 1 |
| Row 2 | 0 |
| Row 3 | 0 |
| Row 4 | 0 |
| ⋮ | |
| Row 24 | 0 |

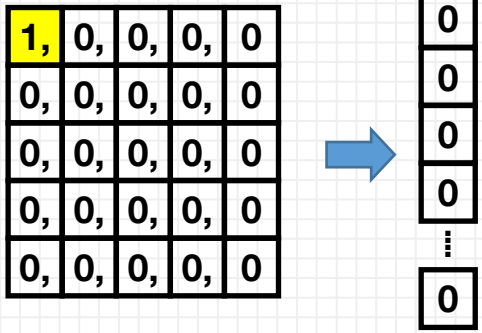
# Generating the Masking Matrix from the Masks

mask0

| | | | | |
|---|---|---|---|---|
| 1, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |

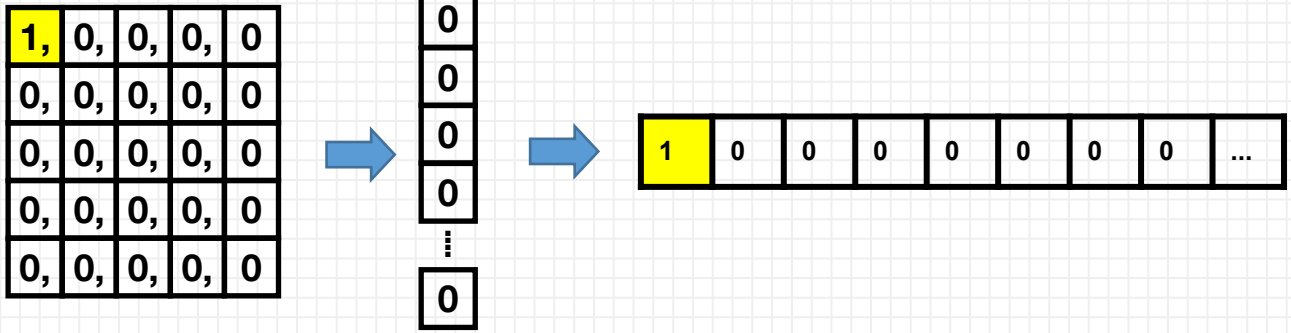
# Generating the Masking Matrix from the Masks

mask0



# Generating the Masking Matrix from the Masks

mask0



# Generating the Masking Matrix from the Masks

mask1

| | | | | |
|---|---|---|---|---|
| 0, | 1, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | ... |

# Generating the Masking Matrix from the Masks

mask1

| | | | | |
|---|---|---|---|---|
| 0, | 1, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |

| |
|---|
| 0 |
| 1 |
| 0 |
| 0 |
| 0 |
| ⋮ |
| 0 |

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | ... |

# Generating the Masking Matrix from the Masks

mask1

| | | | | |
|---|---|---|---|---|
| 0, | 1, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 0 | | | | | | | | |
| 1 | | | | | | | | |
| 0 | | | | | | | | |
| 0 | | | | | | | | |
| ⋮ | | | | | | | | |
| 0 | | | | | | | | |



| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | ... |

# Generating the Masking Matrix from the Masks

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | ... |

# Generating the Masking Matrix from the Masks

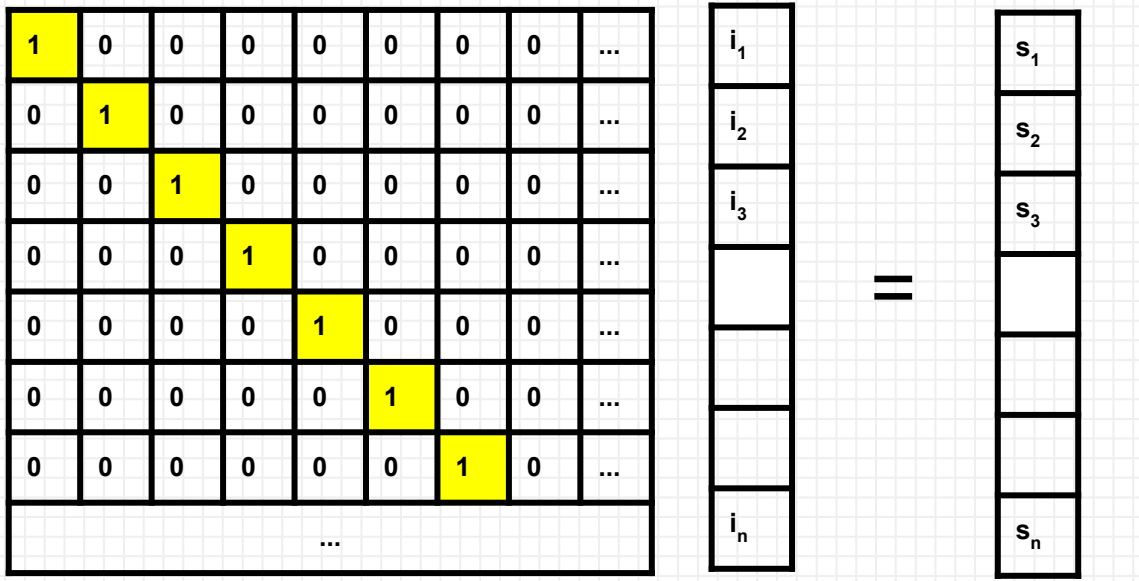
| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | ... |

# Each Row is a Different Experiment

$H =$

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | ... |
| 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | ... |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | ... |
| ... | | | | | | | | |

# Measuring a Pixel is Matrix-Vector Multiplication




Masking Matrix **H**

Unknown, vectorized image, $\vec{i}$

Recorded Sensor readings, $\vec{s}$

## Measuring a Pixel is Matrix-Vector Multiplication

$$\vec{s} = H\vec{\imath}$$

- We know H and we have the sensor readings, how do we get the image?
- How do we solve this?
- When can we solve this?
  - Conditions on H

# How Scanning Works: iPython

$H =$

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | ... |
| 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | ... |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | ... |
| ... | | | | | | | | |

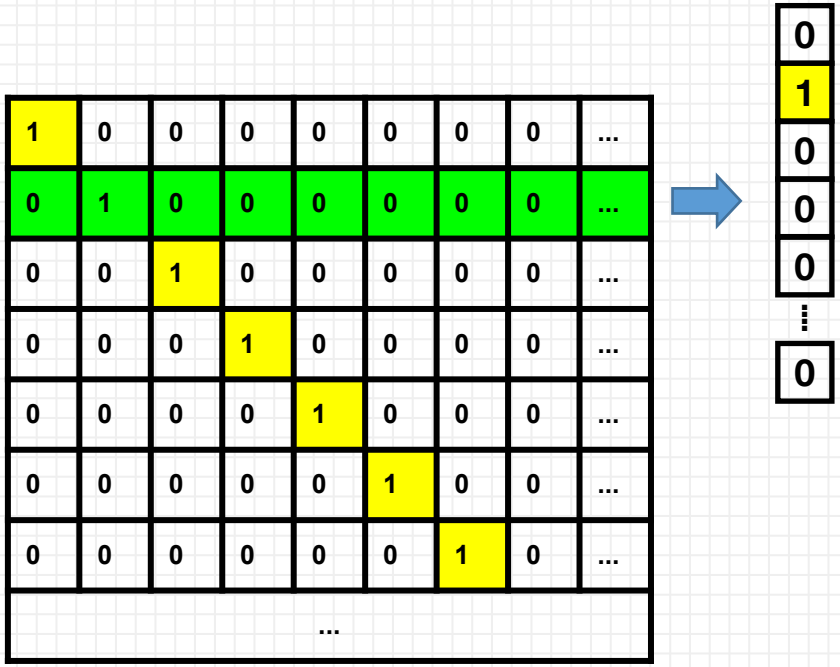
# How Scanning Works: iPython

$H =$

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | ... |
| 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | ... |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | ... |
| ... | | | | | | | | |

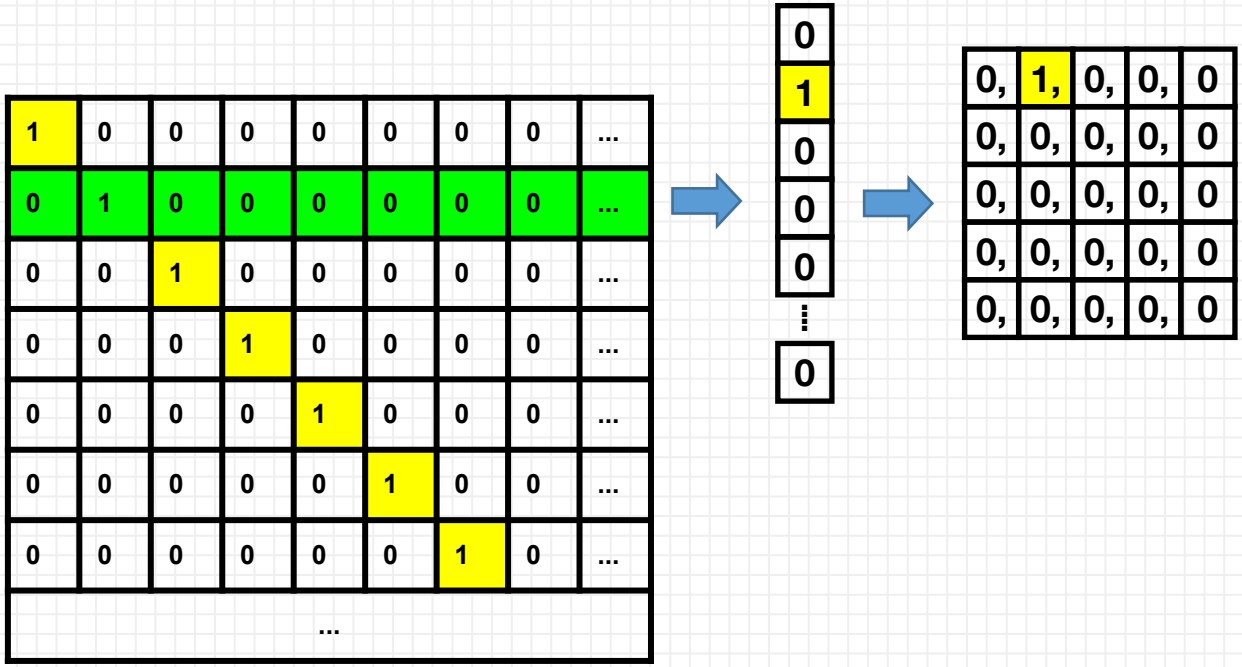
# How Scanning Works: iPython

$H =$



# How Scanning Works: iPython

$H =$



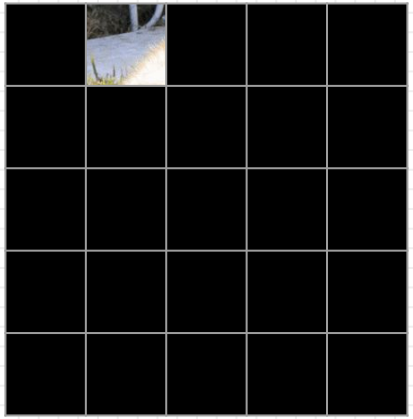
# How Scanning Works: iPython

$H =$

| | | | | | | | | |
|---|---|---|---|---|---|---|---|---|
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | ... |
| 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | ... |
| 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | ... |
| 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | ... |
| ... | | | | | | | | |

| |
|---|
| 0 |
| 1 |
| 0 |
| 0 |
| 0 |
| ⋮ |
| 0 |

| | | | | |
|---|---|---|---|---|
| 0, | 1, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |
| 0, | 0, | 0, | 0, | 0 |

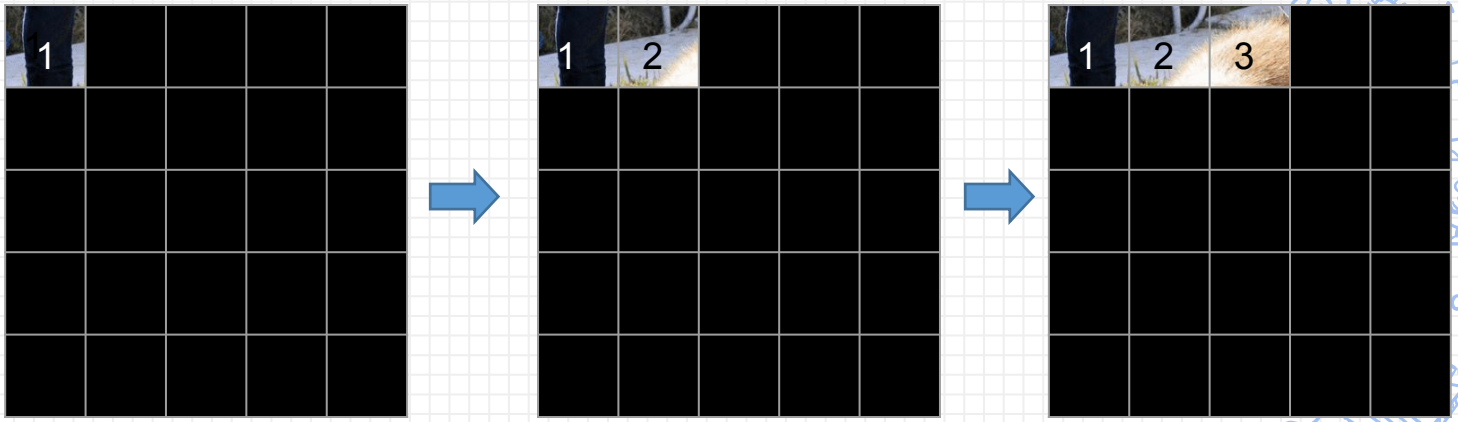


# What Makes a Mask Good?

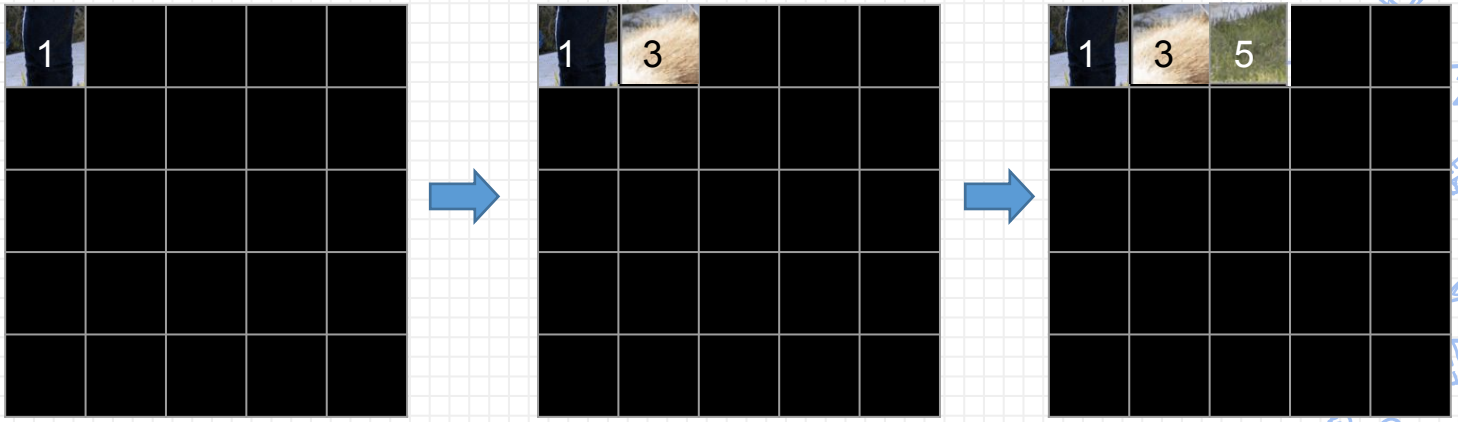
- Linearly independent columns → Invertible
  - Can’t get a solution without this
  - There is a unique solution
- What would be a bad mask?
- Food for thought: Are all invertible matrices equally as good?
  - Find out in Imaging 3 later this week

# Cumulative Scanning

Identity
(H)




Alternating
(H_Alt)



# Important Notes

1. Pick a simple image! Quality can be lost when resizing.
2. Use a short / simple imagePath name
    a. you'll have to fill this in for some cells
    b. default is the home directory for the lab
3. Before starting the simulations, open up the link (in the directions above the code cell) to the display view in a different tab & observe as the cell is running
4. Read simulation descriptions carefully!
    a. you might have to manually set height & width because the defaults are 32x32
5. Each mask section includes ideal + noisy imaging
    a. noisy imaging meant to simulate real projector behavior
    b. don't worry about this for now -- more to come in Img 3