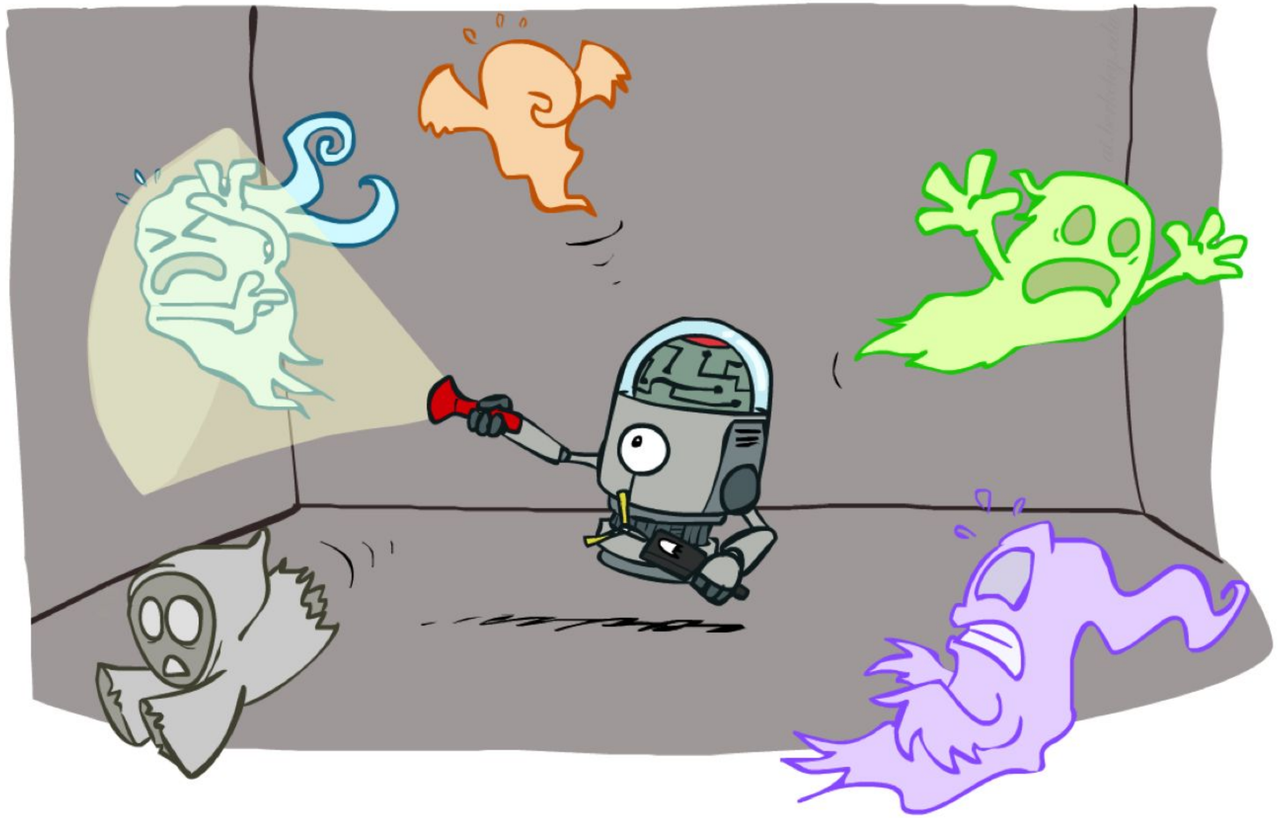
CS 188: Artificial Intelligence

Dynamic Bayes Nets and Particle Filters



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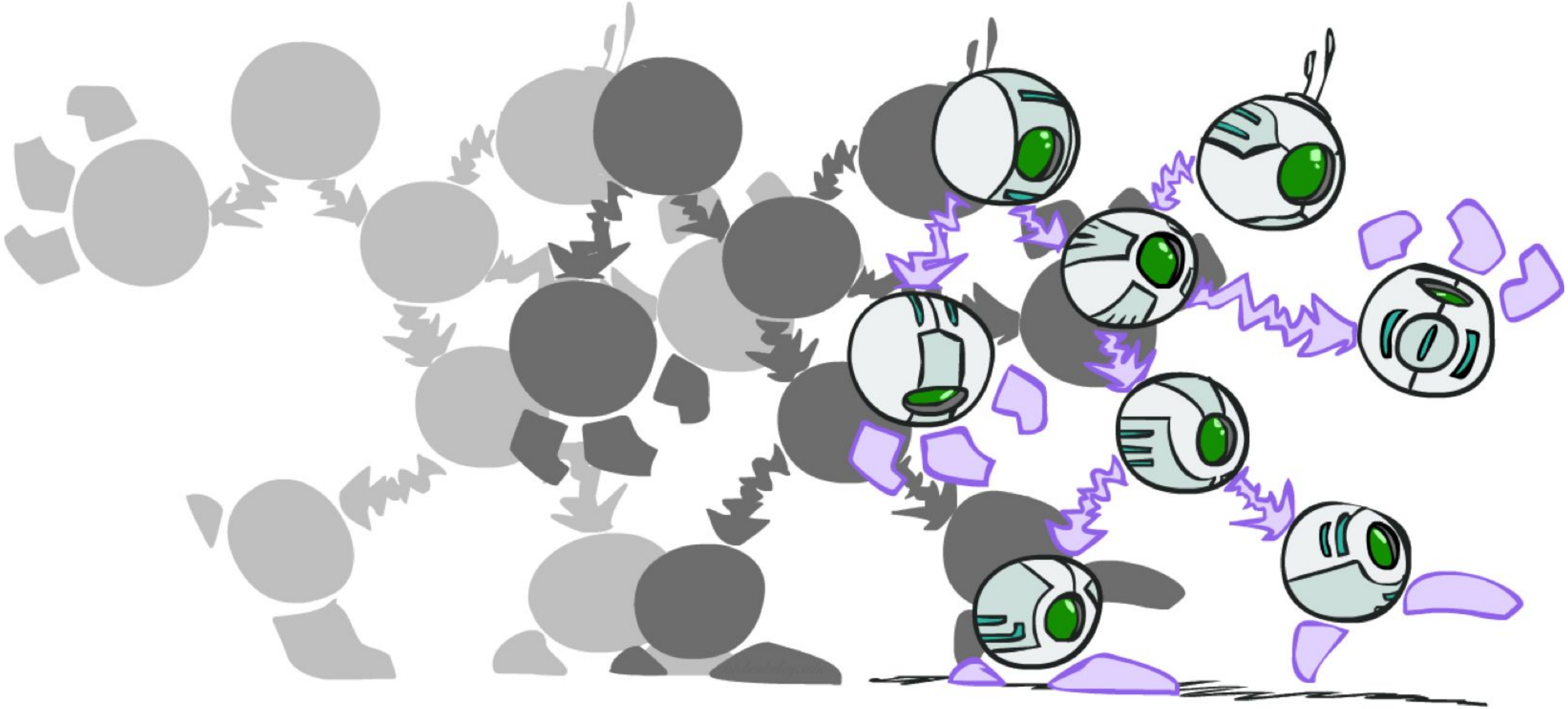
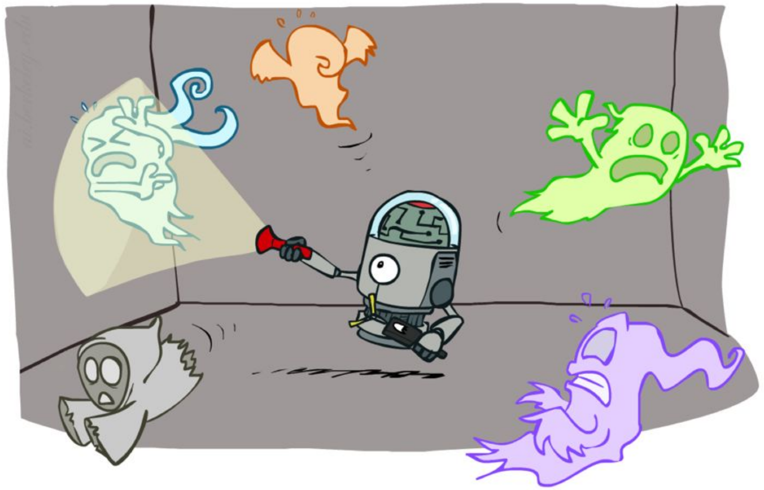
University of California, Berkeley

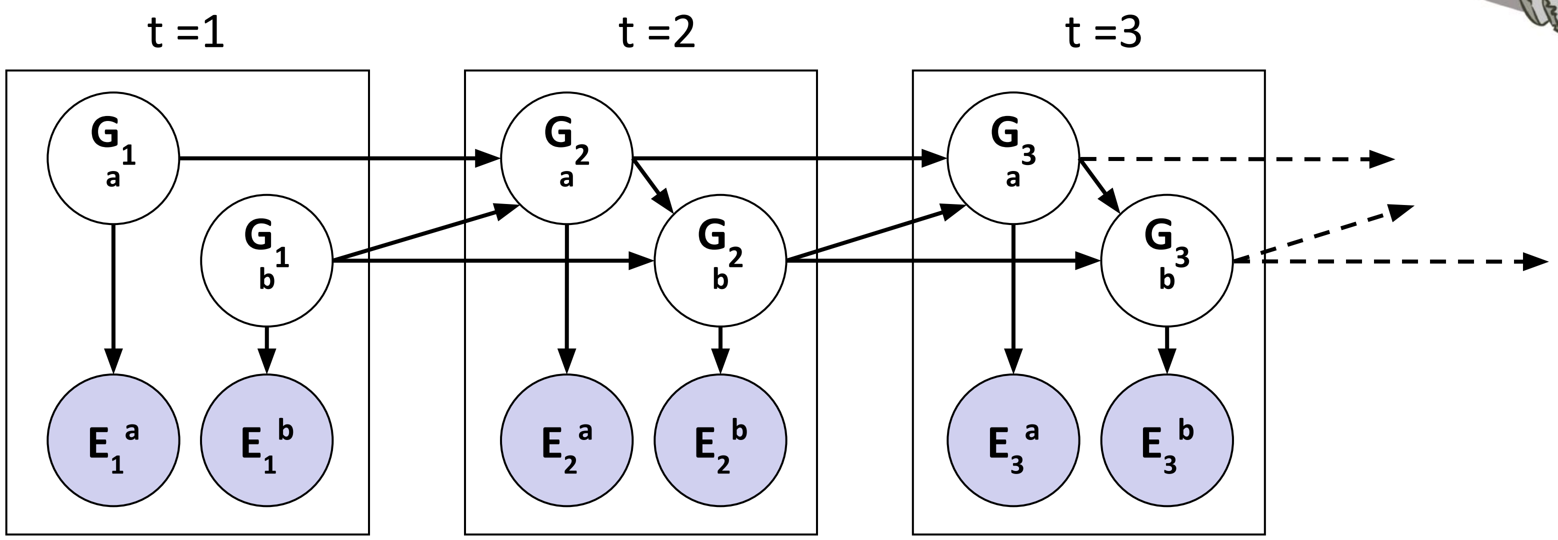
Dynamic Bayes Nets

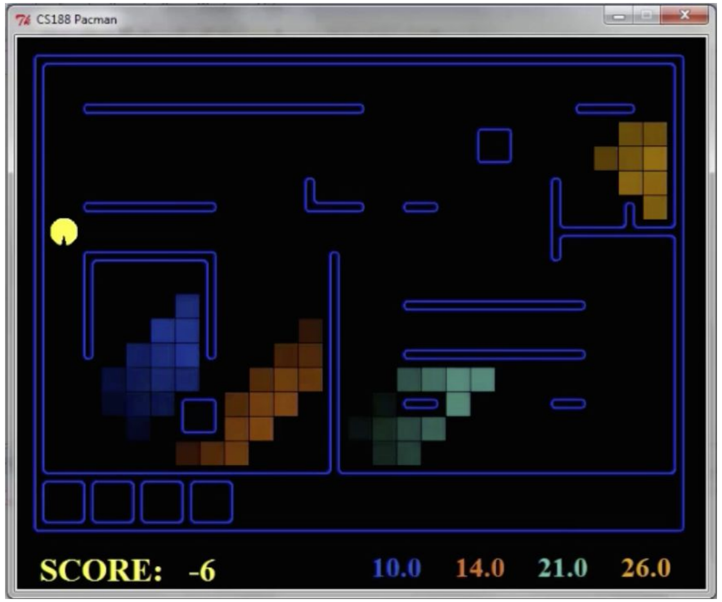


Dynamic Bayes Nets (DBNs)

- We want to track multiple variables over time, using multiple sources of evidence
- Idea: Repeat a fixed Bayes net structure at each time
- Variables at time *t* can have parents at time *t-1*

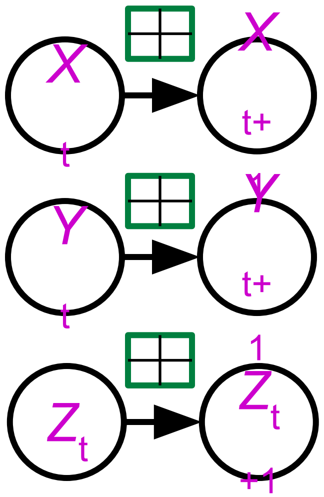


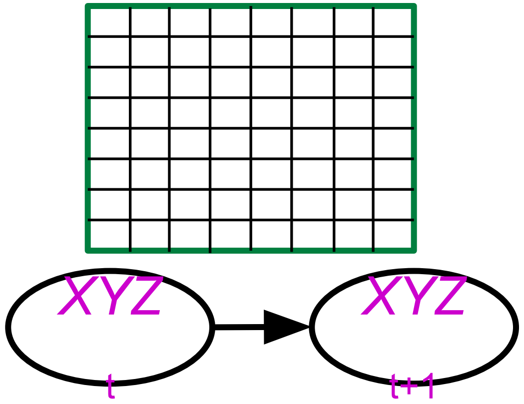




DBNs and HMMs

- Every HMM is a single-variable DBN
- Every discrete DBN is an HMM
  - HMM state is Cartesian product of DBN state variables



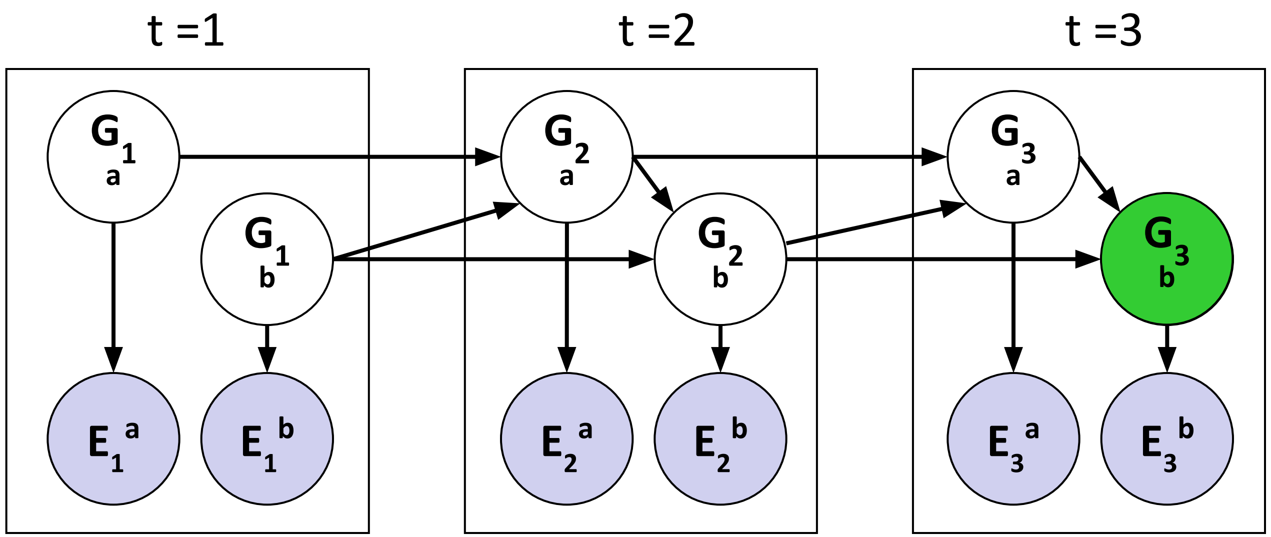


- Sparse dependencies => exponentially fewer parameters in DBN
  - E.g., 20 state variables, 3 parents each;

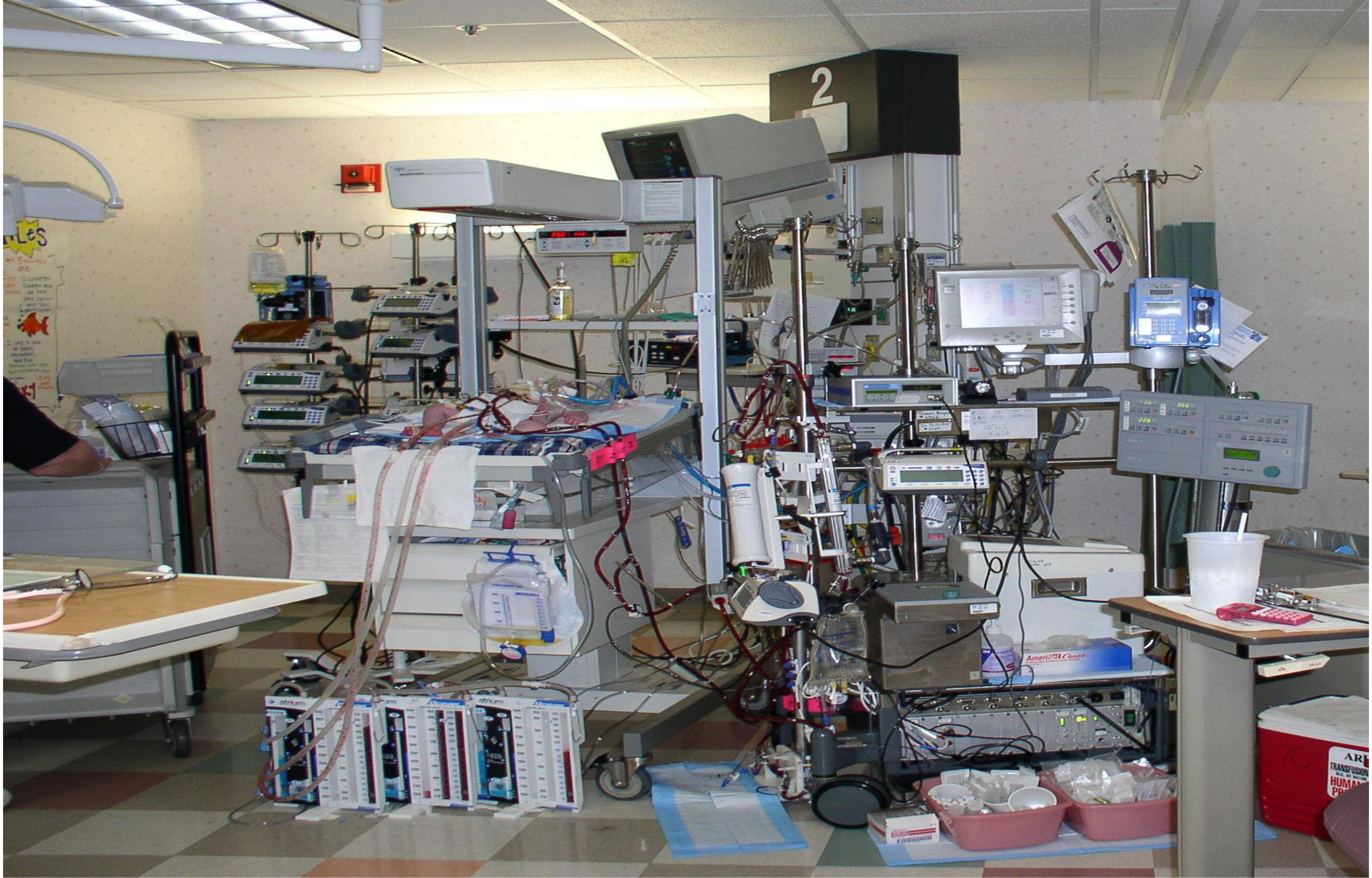
    DBN has 20 x 2^3 = 160 parameters, HMM has 2^{20} x 2^{20} =~ 10^{12} parameters

Exact Inference in DBNs

- Variable elimination applies to dynamic Bayes nets
- Offline: "unroll" the network for T time steps, then eliminate variables to find $P(X_T | e_{1:T})$



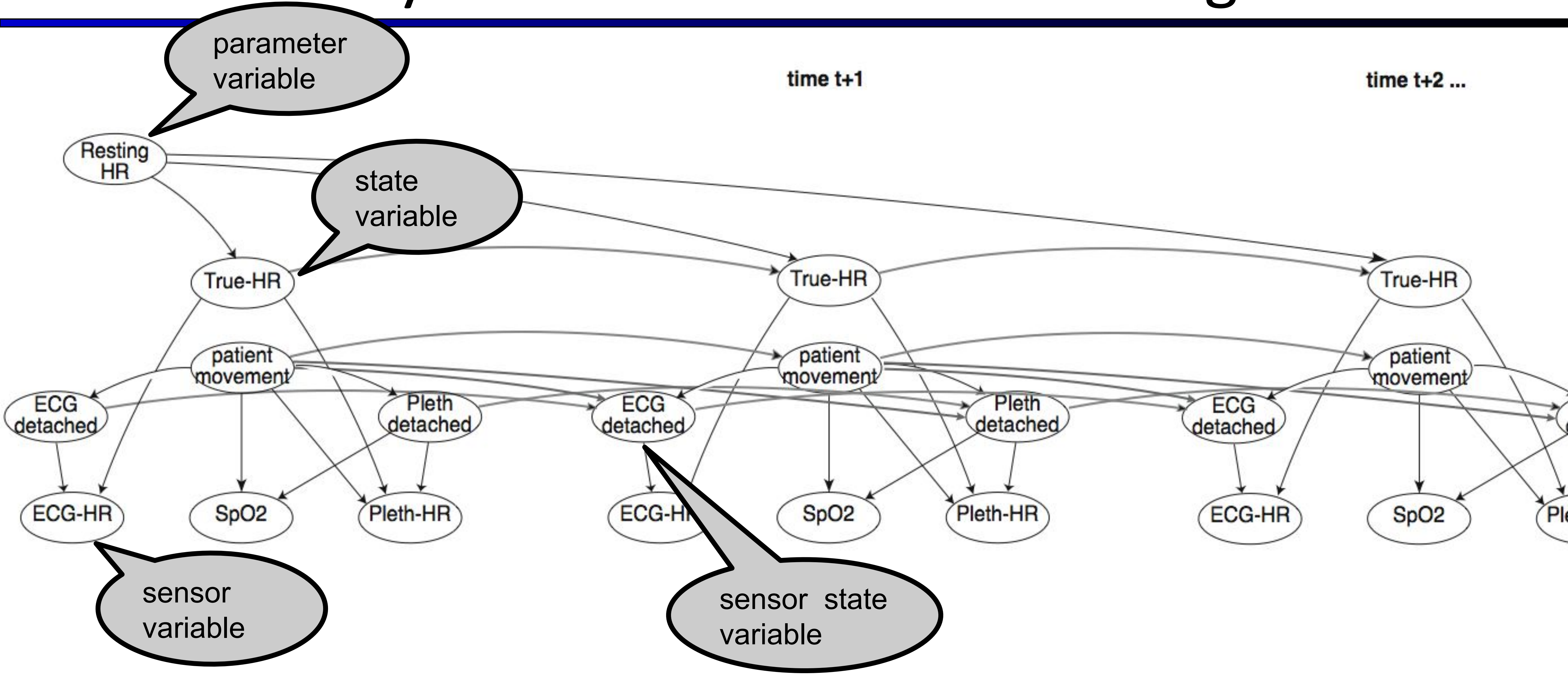
- Online: eliminate all variables from the previous time step; store factors for current time only
- Problem: largest factor contains all variables for current time (plus a few more)


2
atrium

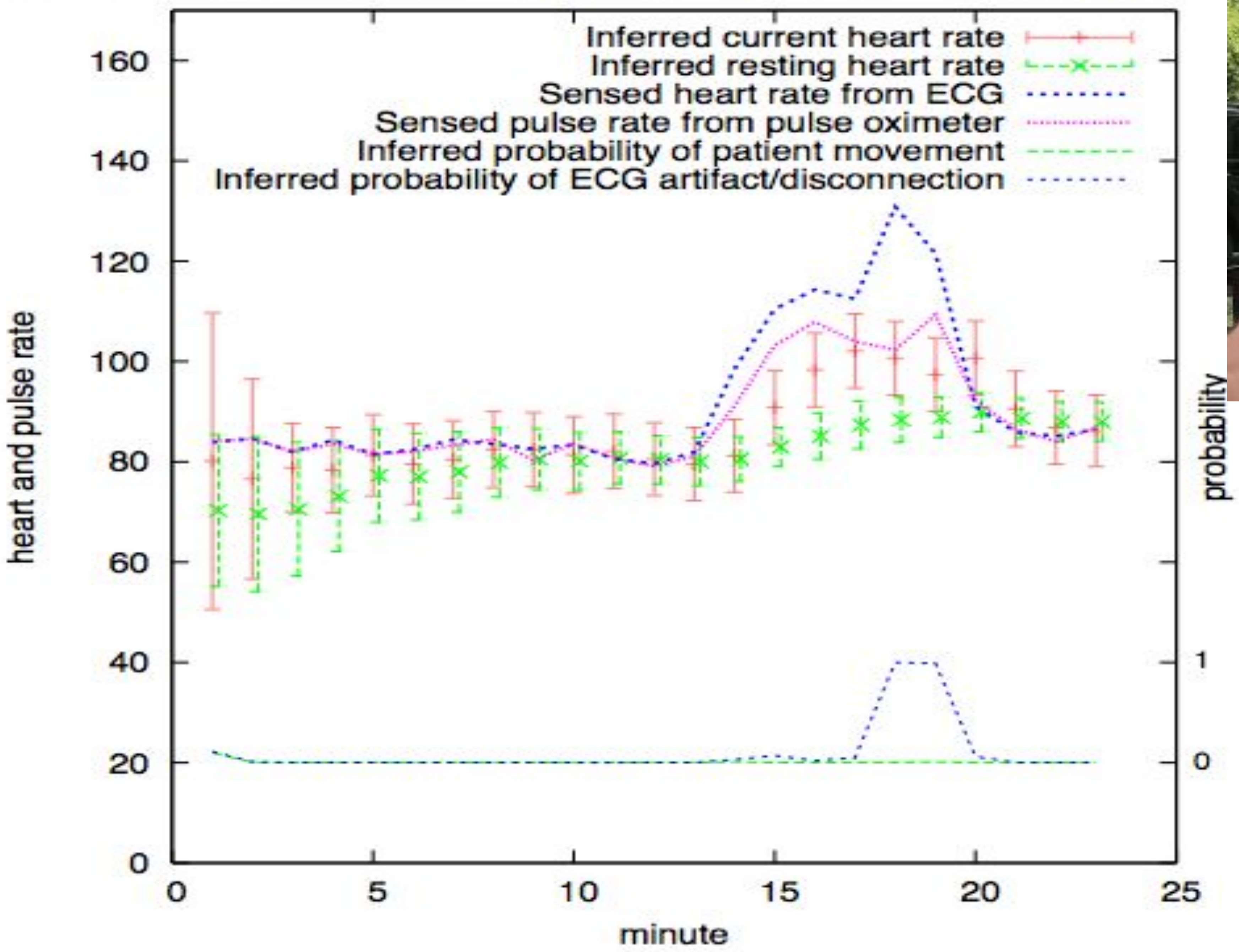
Application: ICU monitoring

- ***State***: variables describing physiological state of patient
- ***Evidence***: values obtained from monitoring devices
- ***Transition model***: physiological dynamics, sensor dynamics
- ***Query variables***: pathophysiological conditions (a.k.a. bad things)

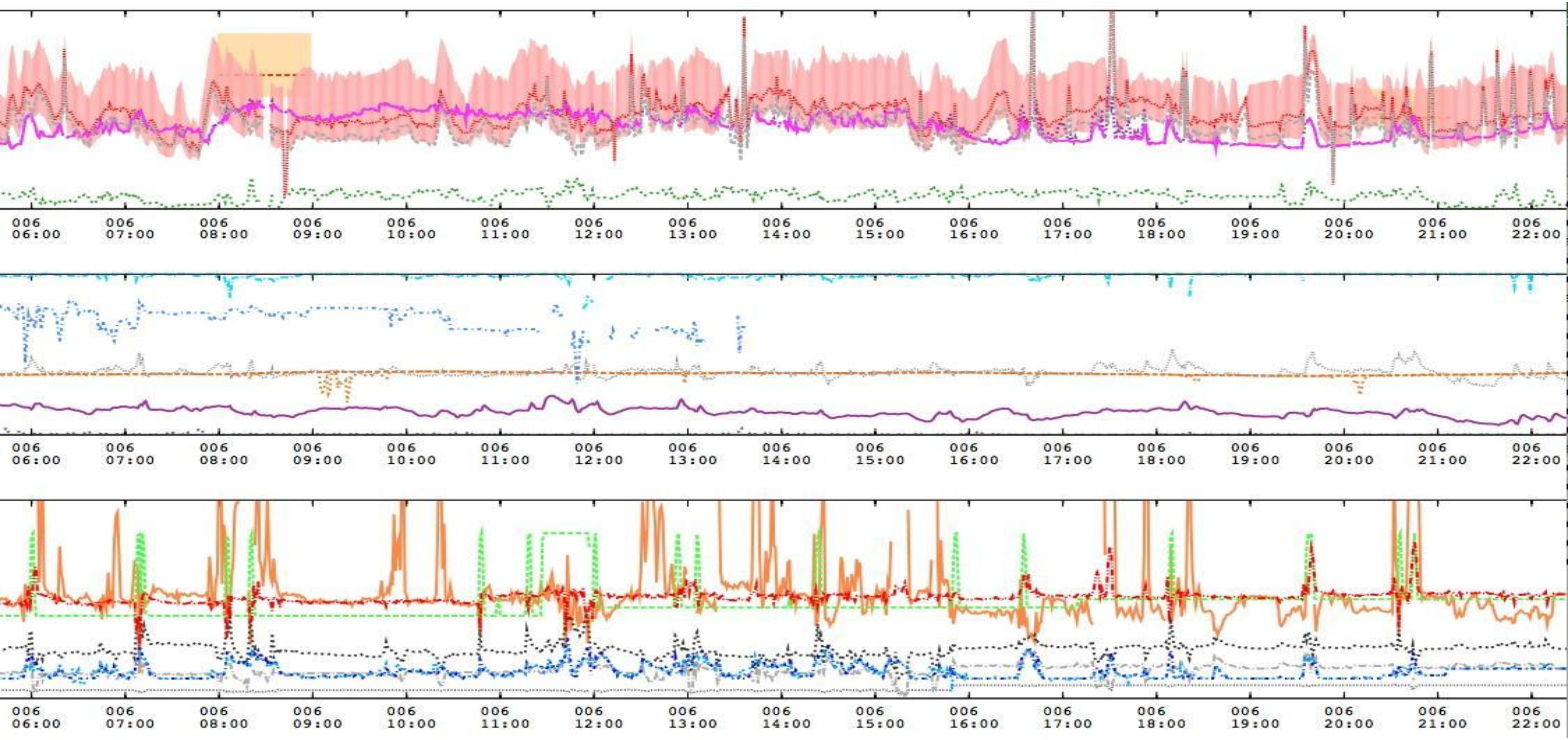
Toy DBN: heart rate monitoring

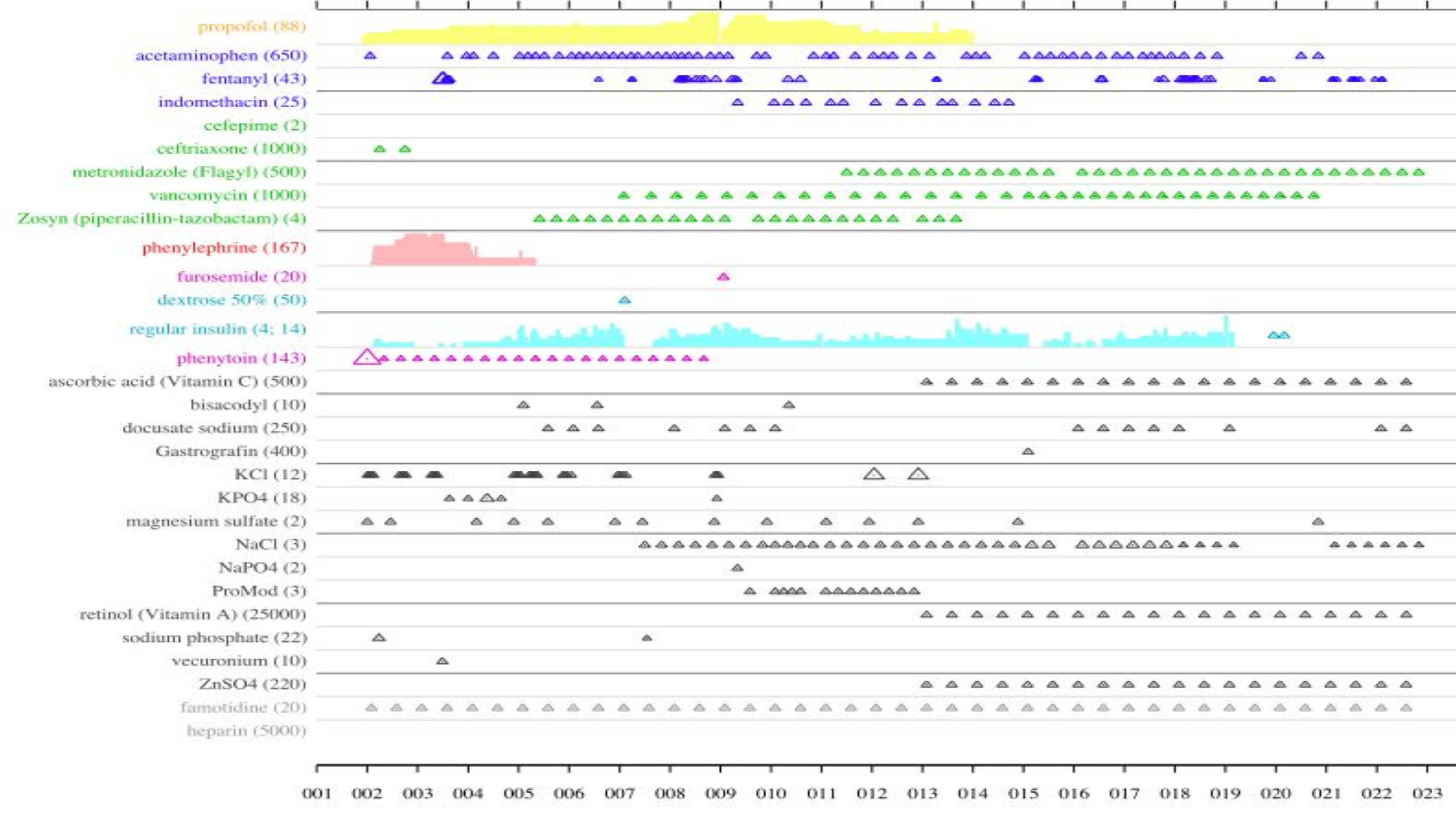


The enhanced heart-rate DBN's inferences on data from a healthy 40-year-o

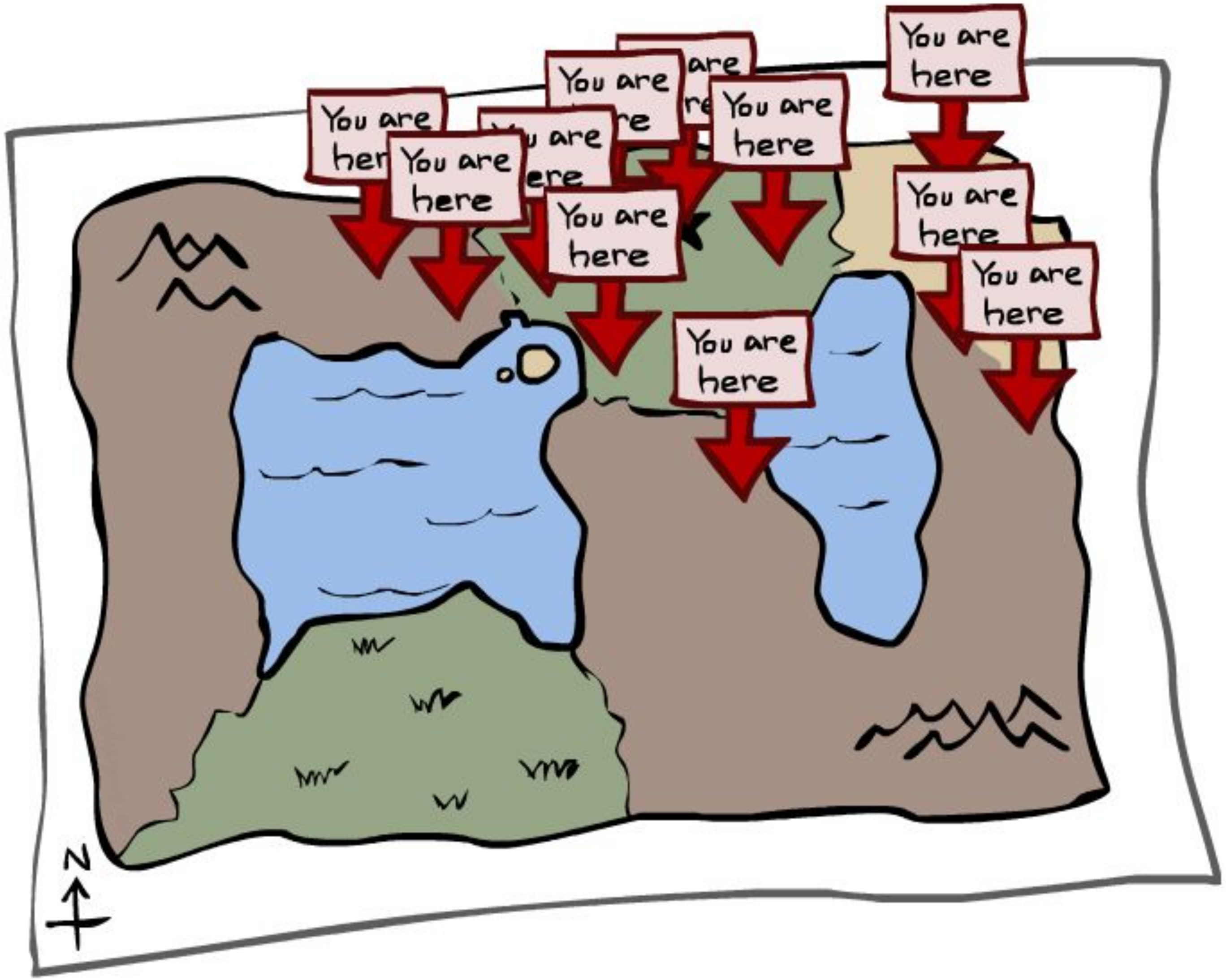


ICU data: 22 variables, 1min ave



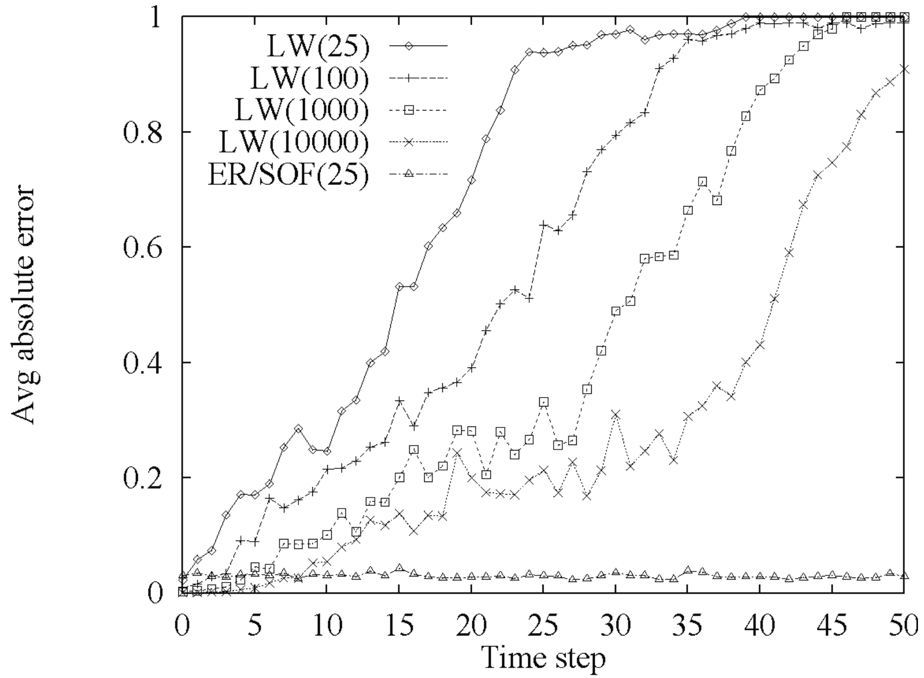

propofol (88)
acetaminophen (650)
fentanyl (43)
indomethacin (25)
cefepime (2)
ceftriaxone (1000)
metronidazole (Flagyl) (500)
vancomycin (1000)
Zosyn (piperacillin-tazobactam) (4)
phenylephrine (167)
furosemide (20)
dextrose 50% (50)
regular insulin (4; 14)
phenytoin (143)
ascorbic acid (Vitamin C) (500)
bisacodyl (10)
docusate sodium (250)
Gastrografin (400)
KCl (12)
KPO4 (18)
magnesium sulfate (2)
NaCl (3)
NaPO4 (2)
ProMod (3)
retinol (Vitamin A) (25000)
sodium phosphate (22)
vecuronium (10)
ZnSO4 (220)
famotidine (20)
heparin (5000)
001 002 003 004 005 006 007 008 009 010 011 012 013 014 015 016 017 018 019 020 021 022 023

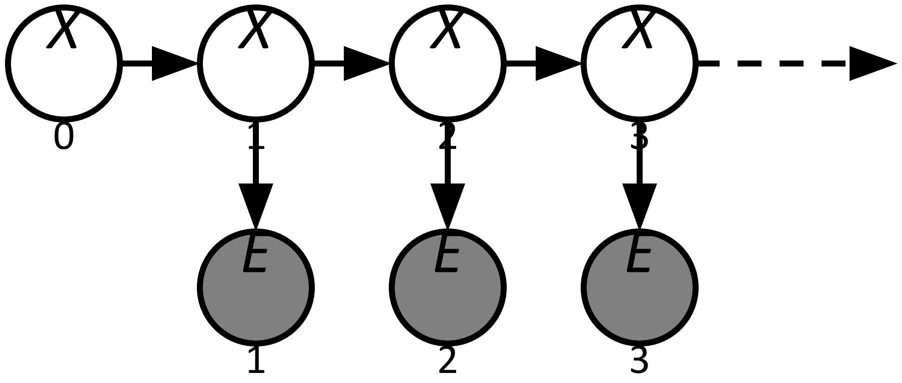
Particle Filtering



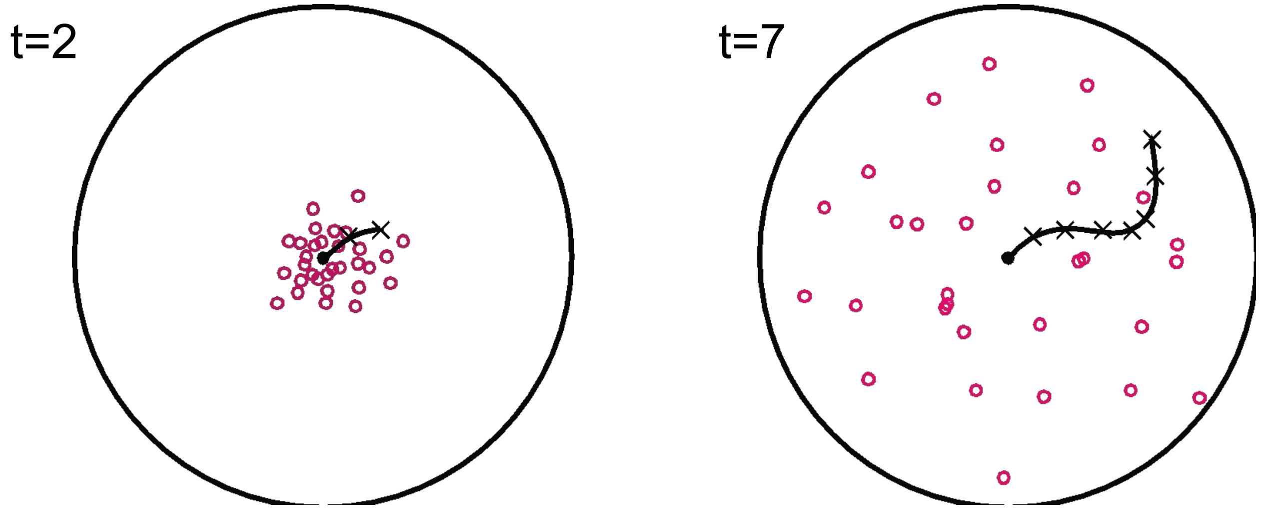
We need a new algorithm!

- When $|X|$ is more than 10^6 or so (e.g., 3 ghosts in a 10x20 world), exact inference becomes infeasible
- Likelihood weighting fails completely – number of samples needed grows ***exponentially*** with T





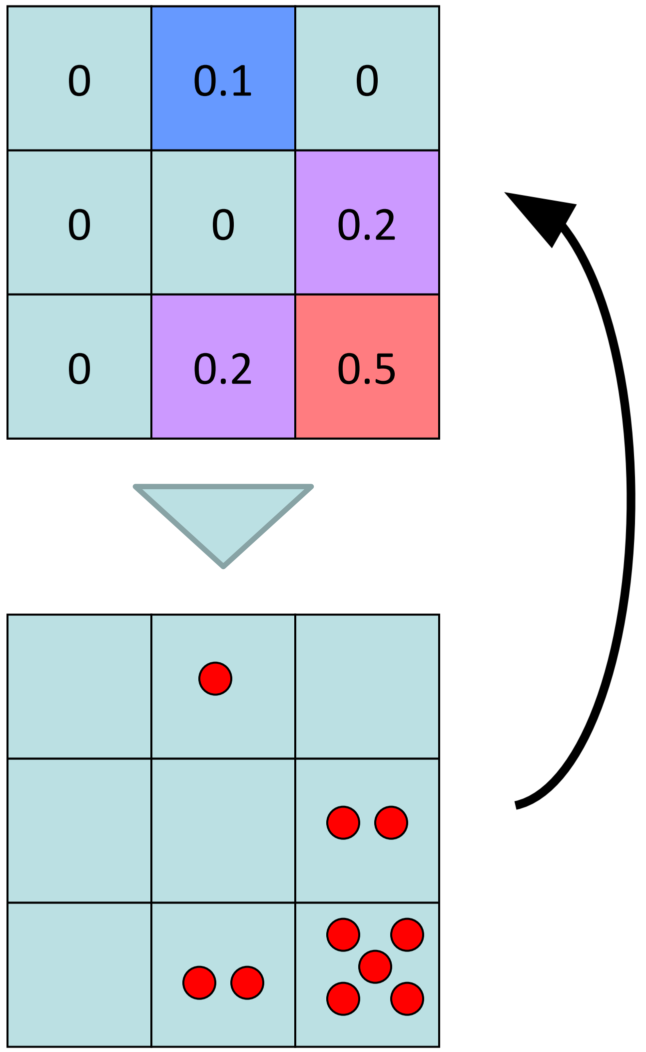
We need a new idea!



- The problem: sample state trajectories go off into low-probability regions, ignoring the evidence; too few "reasonable" samples
- Solution: kill the bad ones, make more of the good ones
- This way the population of samples stays in the high-probability region
- This is called ***resampling*** or survival of the fittest

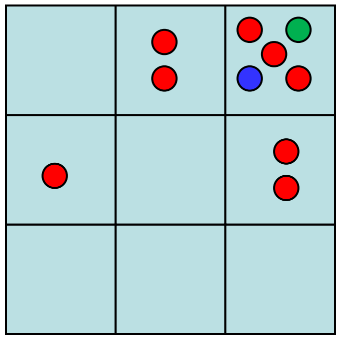
Particle Filtering

- Represent belief state by a set of samples
  - Samples are called ***particles***
  - Time per step is linear in the number of samples
  - But: number needed may be large
- This is how robot localization works in practice



Representation: Particles

- Our representation of $P(X)$ is now a list of $N << |X|$ particles
- $P(x)$ approximated by number of particles with value x
  - So, many x may have $P(x) = 0$!
  - More particles => more accuracy (cf. frequency histograms)
  - Usually we want a ***low-dimensional*** marginal
    - E.g., "Where is ghost 1?" rather than "Are ghosts 1,2,3 in [2,6], [5,6], and [8,11]?"

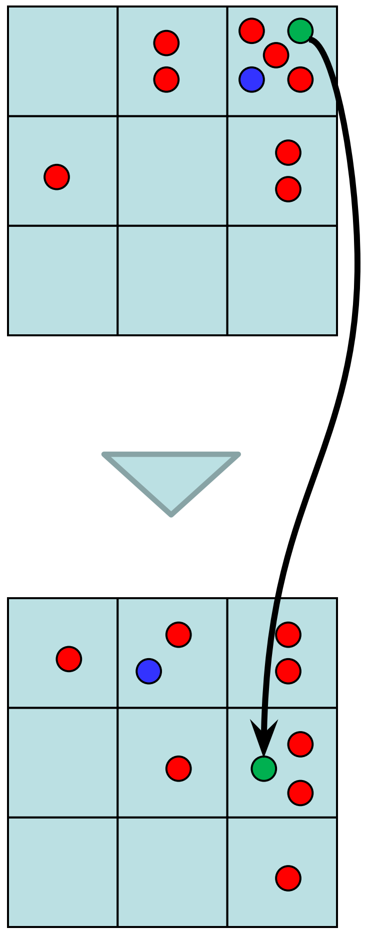


Particles:
(3,3)
(2,3)
(3,3)
(3,2)
(3,3)
(3,2)
(1,2)
(3,3)
(3,3)
(2,3)

Particle Filtering: Prediction step

- Particle j in state $x_t^{(j)}$ samples a new state directly from the transition model:
  - $x_{t+1}^{(j)} \sim P(X_{t+1} \mid x_t^{(j)})$
  - Here, most samples move clockwise, but some move in another direction or stay in place

Particles:
(3,3)
(2,3)
(3,3)
(3,2)
(3,3)
(3,2)
(1,2)
(3,3)
(3,3)
(2,3)

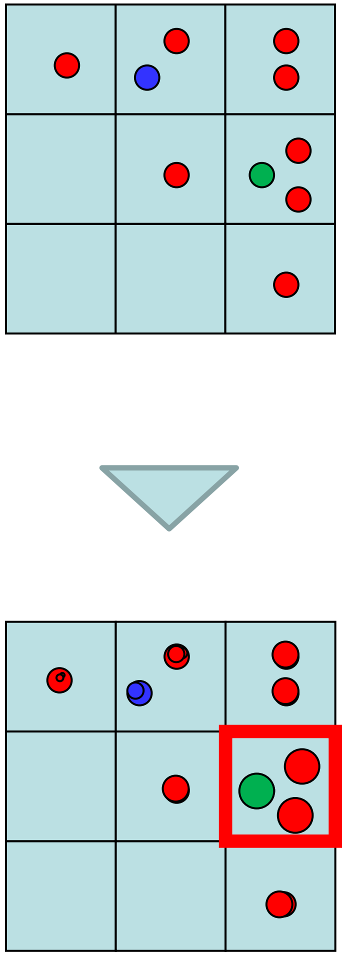


Particles:
(3,2)
(2,3)
(3,2)
(3,1)
(3,3)
(3,2)
(1,3)
(2,3)
(3,2)
(2,2)

Particle Filtering: Update step

- After observing e_{t+1} :
  - As in likelihood weighting, weight each sample based on the evidence
    - $w^{(j)} = P(e_{t+1} \mid x_{t+1}^{(j)})$
  - Normalize the weights: particles that fit the data better get higher weights, others get lower weights

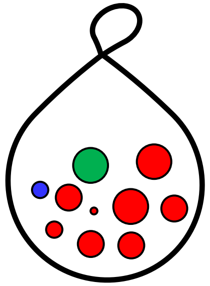
Particles:
(3,2)
(2,3)
(3,2)
(3,1)
(3,3)
(3,2)
(1,3)
(2,3)
(3,2)
(2,2)



Particles:
(3,2) w=.9
(2,3) w=.2
(3,2) w=.9
(3,1) w=.4
(3,3) w=.4
(3,2) w=.9
(1,3) w=.1
(2,3) w=.2
(3,2) w=.9
(2,2) w=.4

Particle Filtering: Resample

- Rather than tracking weighted samples, we ***resample***
- *N* times, we choose from our weighted sample distribution (i.e., draw with replacement)
- Now the update is complete for this time step, continue with the next one (with weights reset to 1)

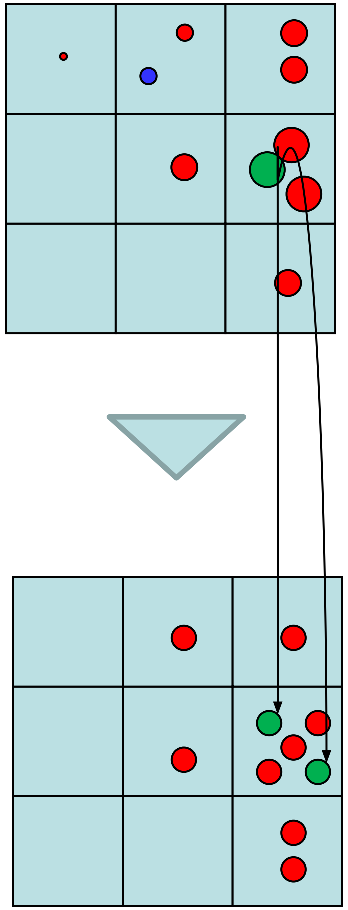


Particles:

(3,2) w=.9
(2,3) w=.2
(3,2) w=.9
(3,1) w=.4
(3,3) w=.4
(3,2) w=.9
(1,3) w=.1
(2,3) w=.2
(3,2) w=.9
(2,2) w=.4

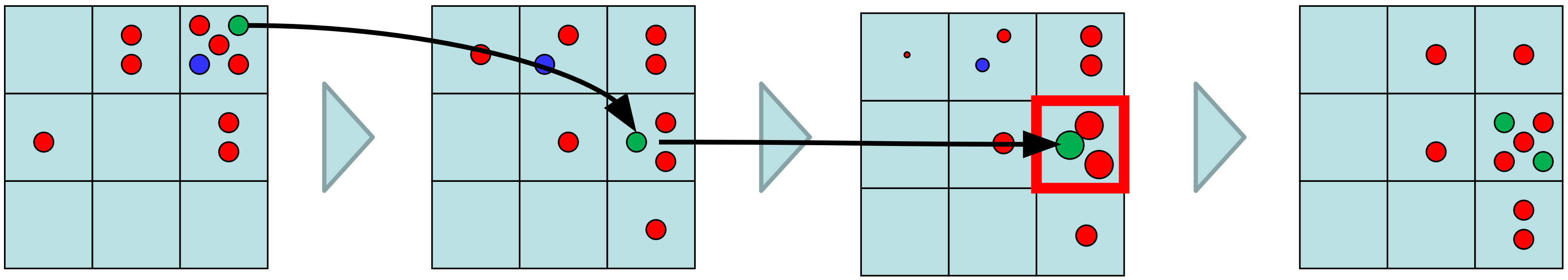
(New) Particles:

(3,2)
(2,2)
(3,2)
(2,3)
(3,3)
(3,2)
(1,3)
(2,3)
(3,2)
(3,2)



Summary: Particle Filtering

- Particles: track samples of states rather than an explicit distribution

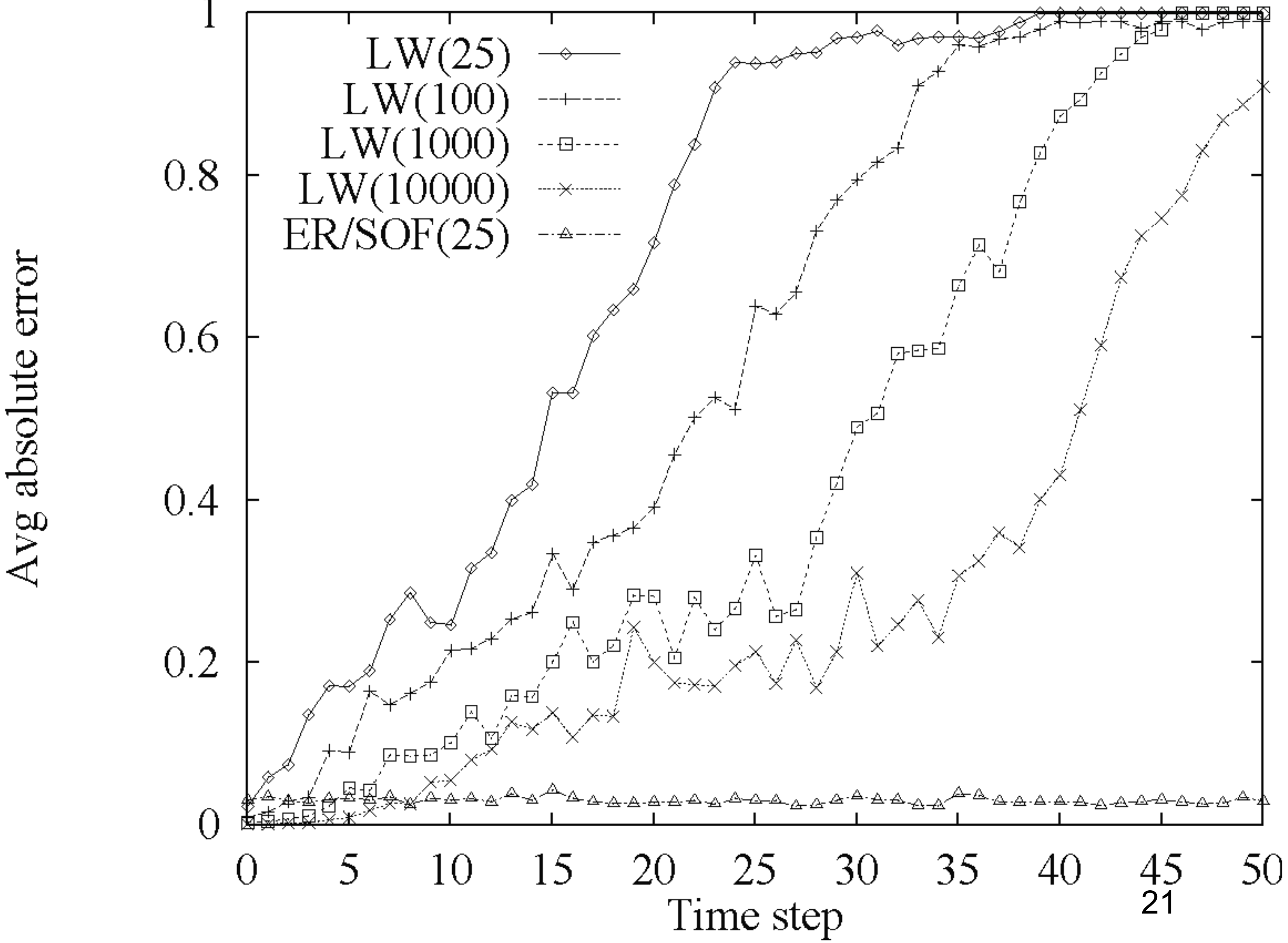


Particles:	Particles:	Particles:	(New) Particles:
(3,3)	(3,2)	(3,2) w=.9	(3,2)
(2,3)	(2,3)	(2,3) w=.2	(2,2)
(3,3)	(3,2)	(3,2) w=.9	(3,2)
(3,2)	(3,1)	(3,1) w=.4	(2,3)
(3,3)	(3,3)	(3,3) w=.4	(3,3)
(3,2)	(3,2)	(3,2) w=.9	(3,2)
(1,2)	(1,3)	(1,3) w=.1	(1,3)
(3,3)	(2,3)	(2,3) w=.2	(2,3)
(3,3)	(3,2)	(3,2) w=.9	(3,2)
(2,3)	(2,2)	(2,2) w=.4	(3,2)

Consistency: see proof in AIMA Ch. 14

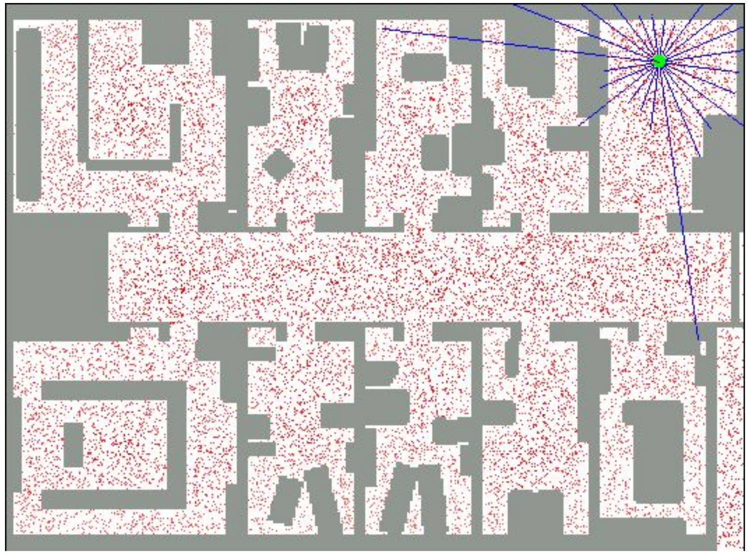
[Demos: ghostbusters particle filtering (L15D3,4,5)]

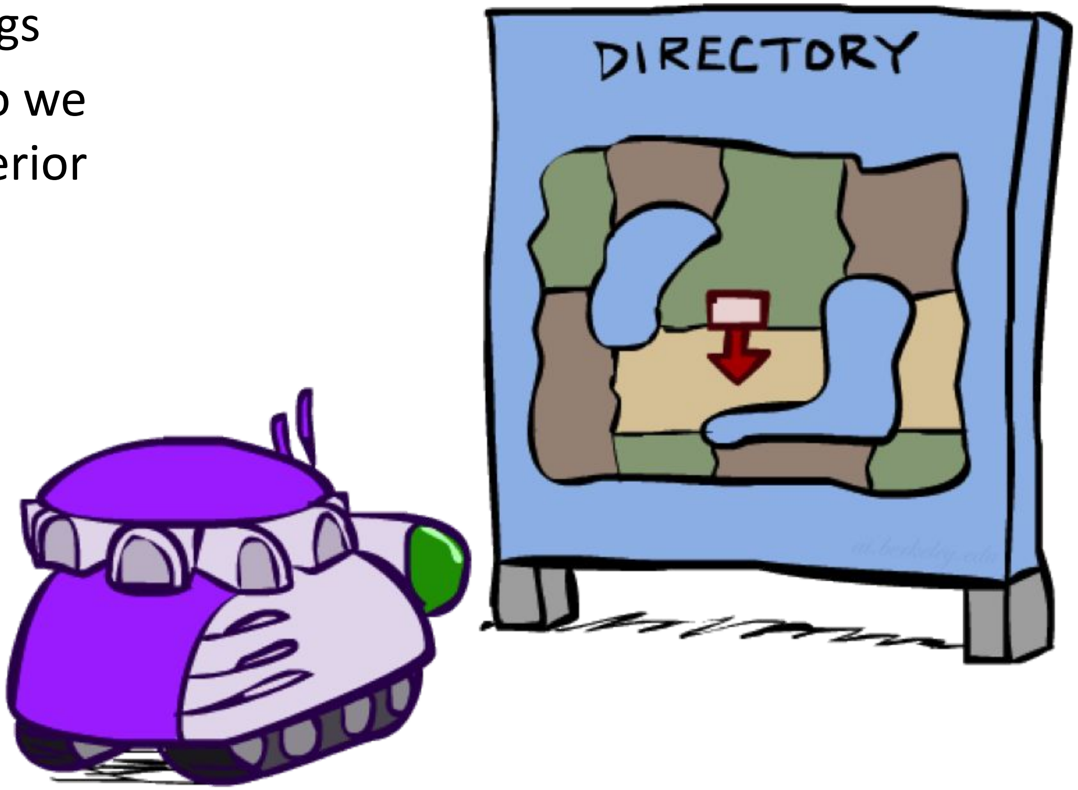
Particle filtering on umbrella model



Robot Localization

- In robot localization:
  - We know the map, but not the robot's position
  - Observations may be vectors of range finder readings
  - State space and readings are typically continuous so we cannot usually represent or compute an exact posterior
  - Particle filtering is a main technique



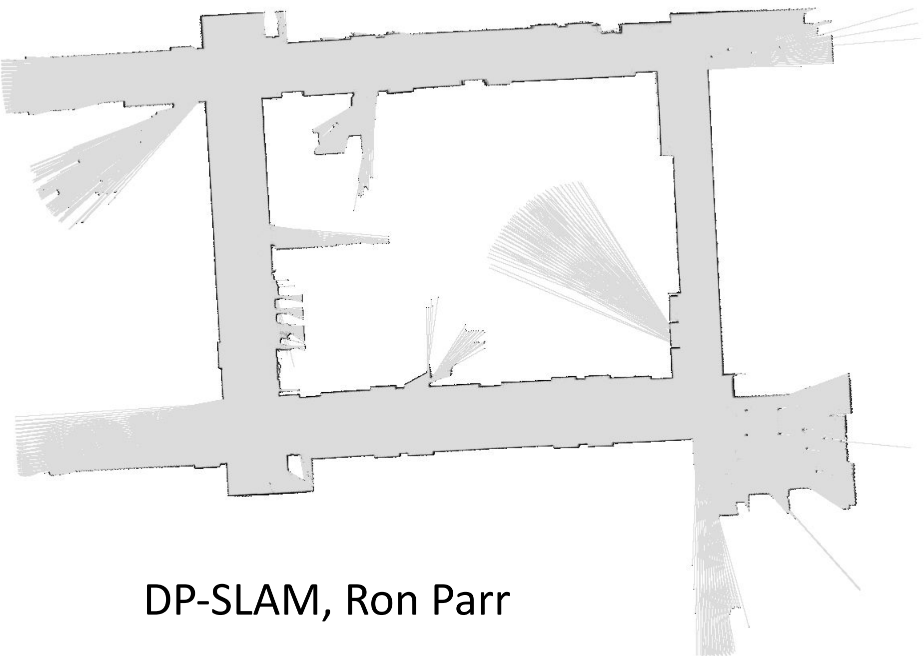


Particle Filter Localization (Sonar)

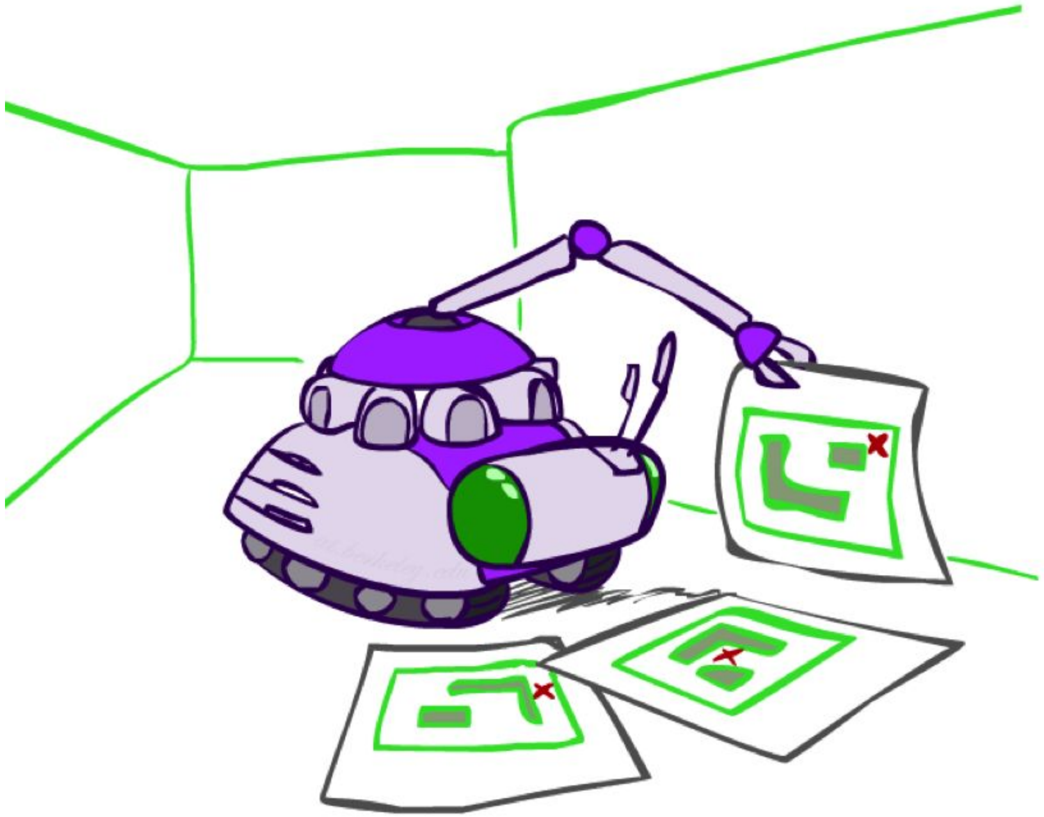
[Video: global-sonar-uw-annotated.avi]

Robot Mapping

- SLAM: Simultaneous Localization And Mapping
  - Robot does not know map or location
  - State $x_t^{(j)}$ consists of position+orientation, map!
  - (Each map usually inferred exactly given sampled position+orientation sequence)

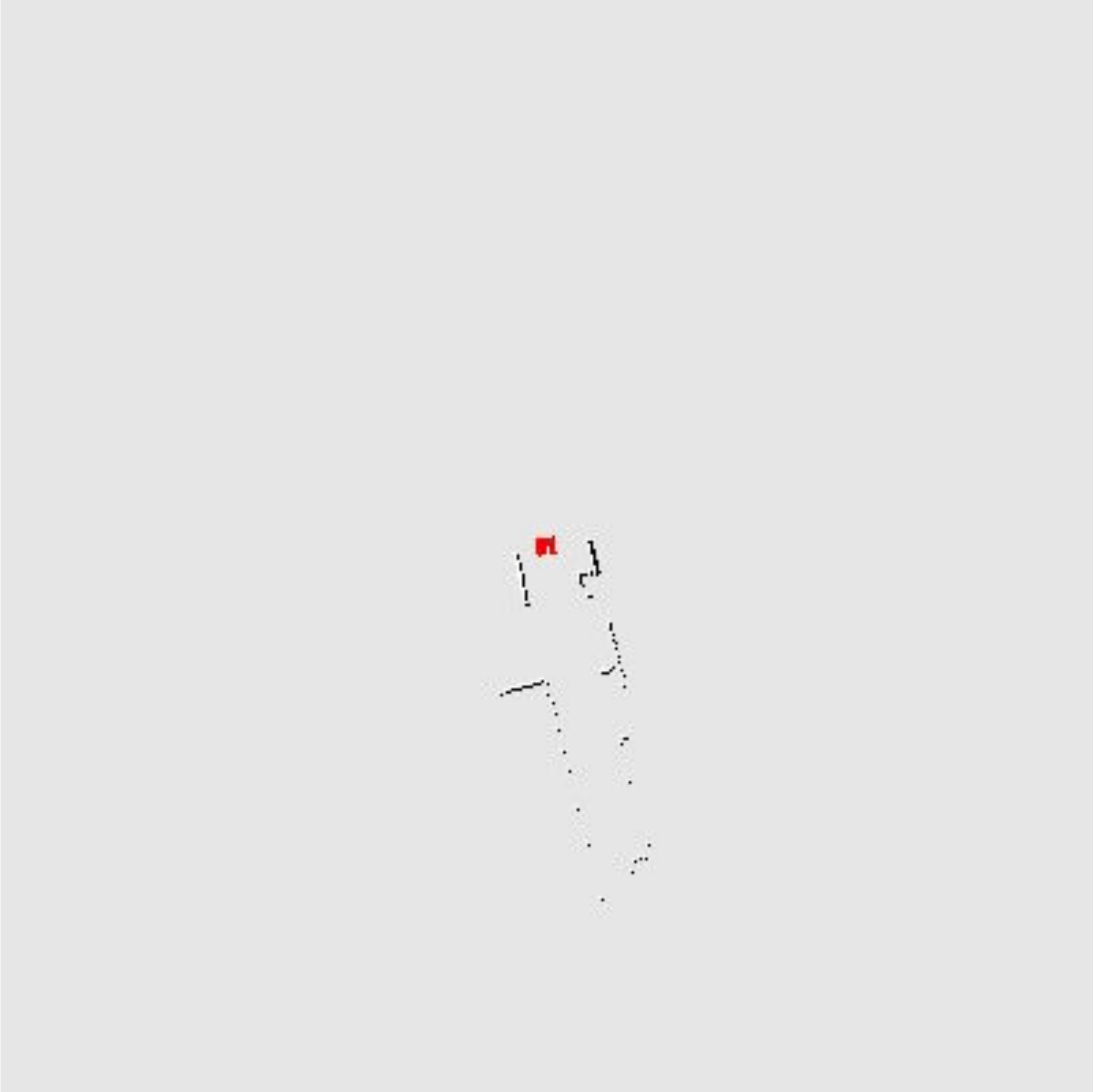


DP-SLAM, Ron Parr



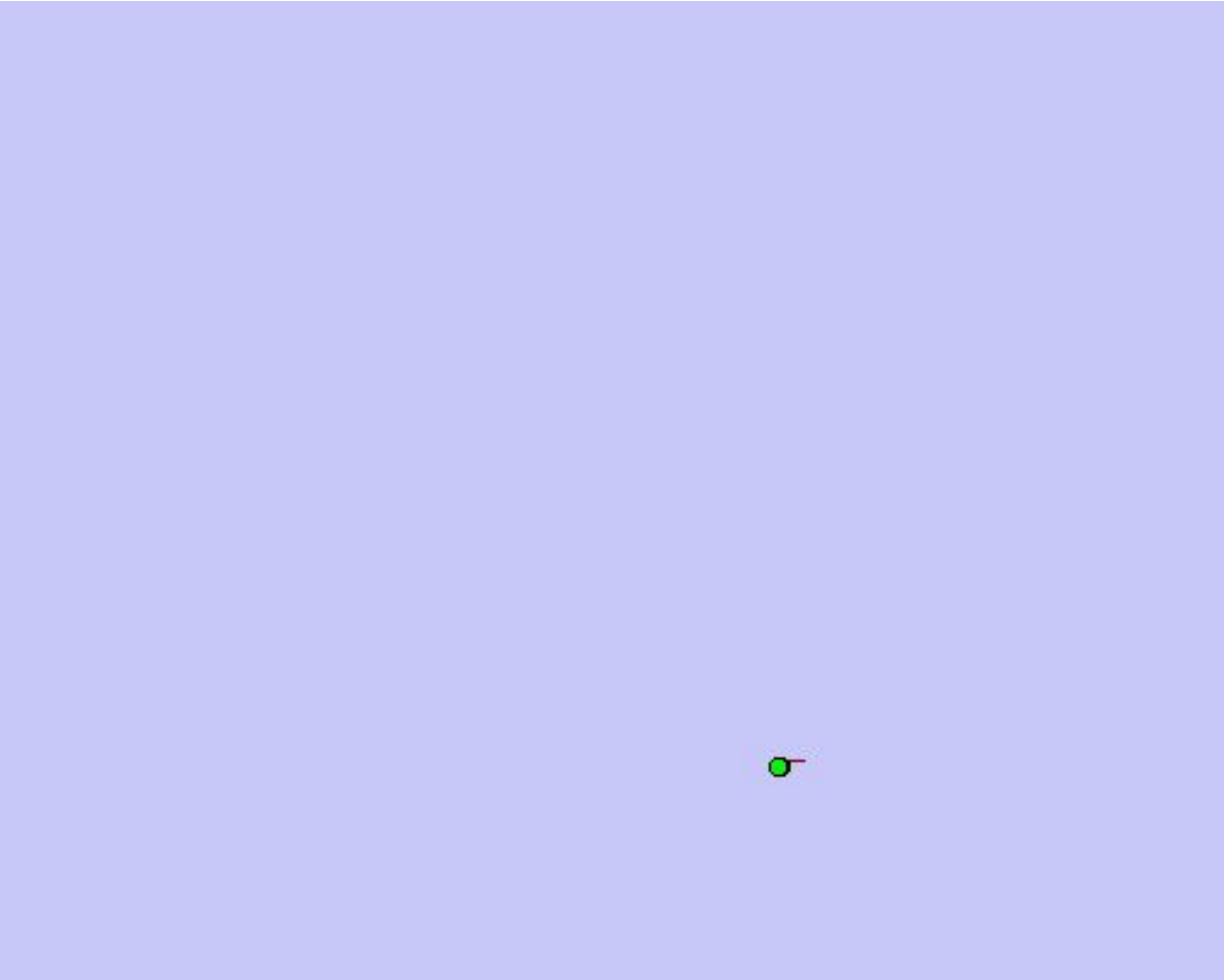
[Demo: PARTICLES-SLAM-mapping1-new.avi]

Particle Filter SLAM – Video 1



[Demo: PARTICLES-SLAM-mapping1-new.avi]

Particle Filter SLAM – Video 2



[Demo: PARTICLES-SLAM-fastslam.avi]